Repton Manor Primary School Maths Calculation Policy 2022-2023

Including Vocabulary Progression



Repton Manor Primary School Calculation Policy 2022-2023

This policy supports the White Rose maths scheme used throughout the school. Progression within each area of calculation is in line with the programme of study in the 2014 National Curriculum. This calculation policy should be used to support children to develop a deep understanding of number and calculation. This policy has been designed to teach children using concrete, pictorial and abstract representations.

- Concrete representation— a child is first introduced to an idea or skill by acting it out with real objects. This is a 'hands on' component using real objects and is afoundation for conceptual understanding.
- Pictorial representation a child has sufficiently understood the 'hands on' experiences performed and can now relate them to representations, such as a diagram or picture of the problem.
- Abstract representation—a child is now capable of representing problems by using mathematical notation, for example $12 \times 2 = 24$.

It is important that conceptual understanding, supported by the use of representation, is secure for all procedures. Reinforcement is achieved by going back and forth between these representations.

Mathematics Mastery: At the centre of the mastery approach to the teaching of mathematics is the belief that all children have the potential to succeed. They should have access to the same curriculum content and, rather than being extended with new learning, they should deepen their conceptual understanding by tackling challenging and varied problems. Similarly, with calculation strategies, children must not simply rote learn procedures but demonstrate their understanding of these procedures with concrete materials and pictorial representations. This policy outlines the different calculation strategies that should be taught and used in line with the requirements of the 2014 Primary National Curriculum.

How to use the policy: This mathematics policy is a guide for all staff. All teachers have been given the scheme of work from the White Rose Maths Hub and are required to base their planning around their year group's modules and not to move onto a higher year group's scheme work. These modules use the Singapore Maths Methods and are affiliated to the workings of the 2014 Maths Programme of Study. Teachers can use any teaching resources that they wish to use and the policy does not recommend one set of resources over another, rather that, a variety of resources are used.

For each of the four number operations, different strategies are laid out, together with examples of what concrete materials can be used and how, along with suggested pictorial representations. The principle of the concrete-pictorial-abstract (CPA) approach [Build it, Draw it, Solve it] is for children to have a true understanding of a mathematical concept, they need to master all three phases within a year group's scheme of work.

Addition - EYFS

Objectives

Knows that a aroup of things change in quantity when something is added.

- Find the total number of items in two groups by counting all of them.
- Says the number that is one more than a aiven number.
- Finds one more from a group of up to five objects, then ten objects.
- In practical activities and discussion, beginning to use the vocabulary involved in adding.
- Using quantities and objects, they add two single digit numbers and count on to find the answer.
- Solve problems including doubling.

Concrete





Use toys and general classroom resources for children to physically manipulate, group/regroup.



Use specific maths resources such as counters, snap cubes. Numicon etc.



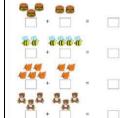


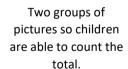


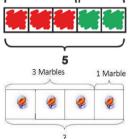
Use visual supports such as ten frames, part part whole and addition mats, with the physical objects and resources that can be manipulated.

Pictorial

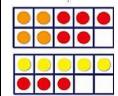




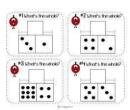


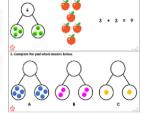


Bar model using visuals, pictures/icons or colours.



Use visual supports such as ten frames. part part whole and addition mats with pictures/icons.

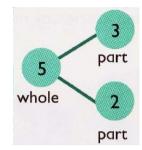


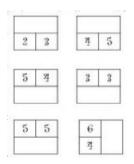


A focus on symbols and numbers to form

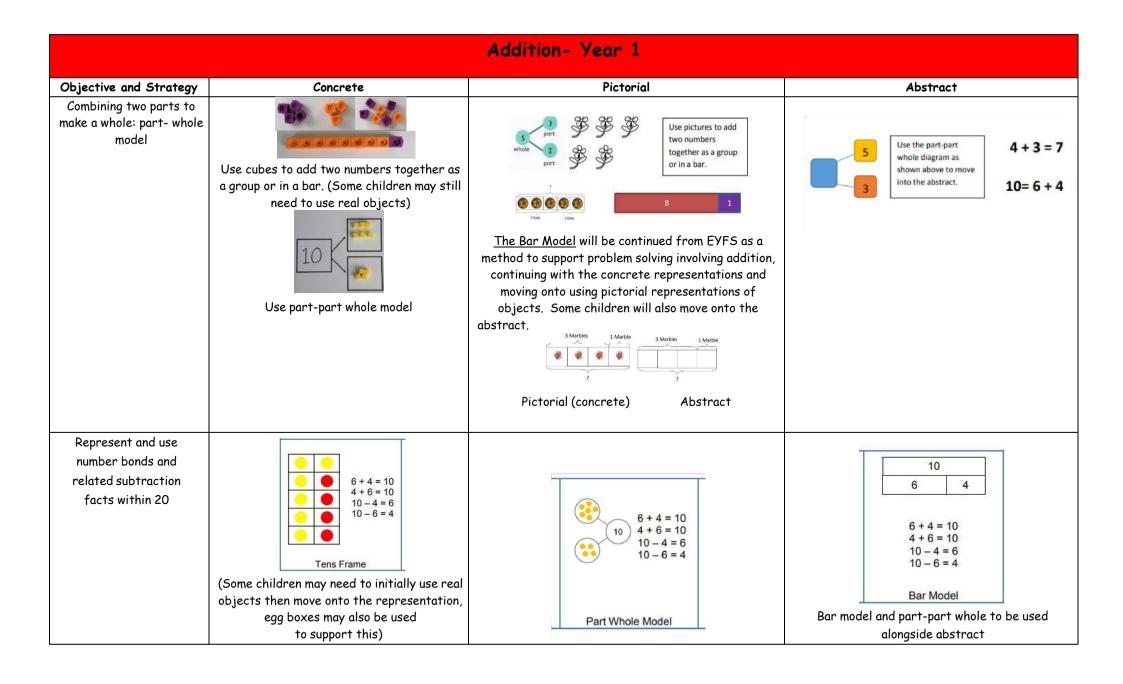
Abstract

a calculation. 5+2=7





* No expectation for children to be able to record a number sentence/addition calculation.



Addition and subtraction of one-digit and two-digit numbers to 20 including 0. Start at the bigger number and counting on	Start with the larger number on the bead string and then count of to the smaller number 1 by 1 to find the answer.	6+3=9 O 1 2 3 4 5 6 7 8 9 10 Start at the larger number on the number line and count on in ones. 12+5=17 Start at the larger number on the number line and count on in ones or in one jump to find the answer.	5 + 12 = 17 17= 12 + 5 Place the larger number in your head and count on the smaller number to find your answer.
Regrouping to make 10 (The 'Make 10' strategy)	Start with the bigger number and use the smaller number to make 10. Use ten frames.	Use pictures or a number line. Regroup or Partition the smaller number using the part part whole model to make 10. 9 + 5 = 14	7 + 4= 11 If I am at seven, how many more do I need to make 10. How many more do I add on now?
Vocabulary	add, more, plus, and, make, altogether, total, equal to, equals, double, most, count on, number line, balancing, part, part, whole		

	Addit	ion- Year 2	
Objective and Strategy	Concrete	Pictorial	Abstract
Adding 3 1-digit numbers	4 + 7 + 6= 17 Put 4 and 6 together to make 10. Add on 7. Following on from making 10, make 10 with 2 of the digits (if possible) then add on the third digit.	Add together three groups of objects. Draw a picture to recombine the groups to make 10.	4 + 7 + 6 = 10 + 7 $= 17$ Combine the two numbers that make 10 and then add on the remainder.
Adding a 2-digit number			
and ones	Use ten frame to make 'magic ten Children explore the pattern. 17 + 5 = 22 27 + 5 = 32	Use part part whole and number line to model. 17 + 5 = 22 3 2 16 + 7	
	2/+5=32	? 15 3	17 + 5 = 22
		2 44 11	Explore related facts
		Bar Model	17 + 5 = 22
			5 + 17 = 22
			22—17 = 5
			22—5 = 17

		07 : 00	
Adding a 2-digit number		27 + 30	
and multiples of 10		+10 +10 +10	27 + 10 = 37
			27 + 20 = 47
	25 + 10 = 35	+ + + +	
	Explore that the ones digit does not change	27 27 47 57	27 + 🗆 = 57
		27 37 47 57	
		Base 10 may be used above the number line initially.	
		The calculation will be shown alongside the	
		number line to see the connection	
Adding two 2-digit numbers	24 + 15= Add together the ones first then add the tens. Use the Base 10 blocks first	After practically using the base 10 blocks and place value counters, children can draw the counters to help them to solve additions.	
(No re-grouping)	before moving onto place value counters.	то	25 ± 47.
	T 0		20 + 5 40 + 7
			20 + 40 = 60
			5+ 7 =12
	(Some children may not be ready for place value	+20 +5 Or +20 +3 +2	60 + 12 = 72
	counters in Y2)	47 67 72 47 67 70 72	Partitioning:
	Numicon may also	Use number line and bridge ten using part	
	be used	whole if necessary.	
	PROST PROP =	Base 10 may be used above the number line.	
		The calculation will be shown alongside the	
		number line to see the connection	Recording addition in columns supports place value and prepares for formal
			written methods with larger numbers.
		Model Calculation	Toward the end of the year, children move
			to more formal recording using
			partitioning method: 40 + 7
			30 + 5
		The Bar Model (Singapore maths) will be used	70 + 12
		to support problem solving moving onto the generalisation that b+c=a. Children will focus	
		on using the abstract representation with the	
		pictorial to support where necessary.	
Vocabulary	add, more, plus, and, make, altogether, total, equal to, e	ı cquals, double, most, count on, number line, sum, t	rens, units, partition, addition, column, tens
		boundary	

	Addition	- Year 3	
Objective and Strategy	Concrete	Pictorial	Abstract
Add and subtract numbers with up to 3-digits, using formal written methods of columnar addition Column addition (no regrouping)	Using manipulatives (dienes, numicon, counters), children are to line up hundreds, tens and ones. Children should be secure with using PV counters before moving onto pictorial. The calculation will be shown alongside the model used to see the connection Model Calculation	Children are to draw, in a PV frame, the manipulatives, that they are using. Secure knowledge of representation with the PV columns. The calculation will be shown alongside the model to see the connection Model Calculation	2 2 3 + 1 1 4 3 3 7 Children to move onto recording more formally. Some children may need to use the expanded method (see below).

Column addition (with	Hundreds Tens Ones		
regrouping)		153 William Tera Ones	$\begin{array}{rrrr} 20 & + & 5 \\ \underline{40} & + & 8 \\ \hline 60 & + & 13 & = 73 \end{array}$
		= 5 0	Children are to begin with the abstract: expanded form.
		Children can draw a representation of the	For those children, that are confident
		grid to further support their	after AFL, the below method should be
		understanding, carrying the ten	used.
		underneath the line.	
	115 = 242		$\frac{536}{+85}$ $\frac{621}{11}$
	Exchange ten ones for a ten. Model using Dienes,		
	Numicon and place value counters.		
Vocabulary	addition add, more, and make, sum, total, altogether, double, near double, half, halve, tens boundary, hundreds boundary		

	Addition-	- Year 4	
Objective and Strategy	Concrete	Pictorial	Abstract
Using formal written methods of columnar addition where appropriate add numbers with up to 4 digits (with exchange)	Children continue to use dienes or place value counters to add, exchanging ten ones for a ten and ten tens for a hundred and ten hundreds for a thousand. The calculation will be shown alongside the manipulative used to see the connection Model Calculation Model Calculation	Children can draw a pictorial representation of the columns and place value counters to further support their learning and understanding.	3517 + 396 3913 Continue from previous work to carry hundreds as well as tens.
Add decimals with 2 decimal places, including money.	Introduce decimal place value counters and model exchange for addition.	2.37 + 81.79 +ens	£23 59 + £7 55 £31 1 1 4 As the children move on, introduce decimals with the same number of decimal places and different. Money can be used here.
Vocabulary	addition add, more, and make, sum, total, altogether, d	ouble, near double, half, halve, tens bound point	ary, hundreds boundary, decimal, decimal

Addition- Year 5/6			
Objective and Strategy	Concrete	Pictorial	Abstract
add numbers with more than 4 digits.	See Year 4	See Year 4	Children should have abstract supported by a pictorial or concrete if needed.
add several numbers of increasing complexity, including adding money, measure and decimals with different numbers of decimal points.	See Year 4	See Year 4	8 1,05 9 3,66 8 15,30 1 + 20,551 120,579 11,179 23 · 36 1 9 · 080 59 · 770 + 1 · 300 93 · 511 Insert zeros for place holders.
/ocabulary	addition add, more, and make, sum, total, altogethe	r, double, near double, half, halve decimal point	e, tens boundary, hundreds boundary, decimal,

Subtraction- EYFS

- Knows that a group of things change in quantity when something is taken away

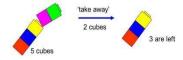
Objectives

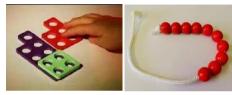
- Find one less from a group of five objects, then ten objects.
- In practical activities and discussion, beginning to use the vocabulary involved in subtracting.
- Using quantities and objects, they subtract two single digit numbers and count back to find the answer.

Concrete



Use toys and general classroom resources for children to physically manipulate, group/regroup.





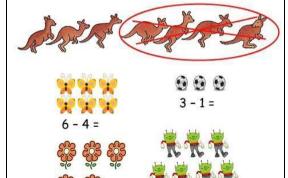
Use specific maths resources such as snap cubes, Numicon, bead strings etc.



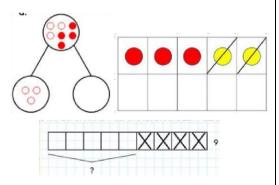


Use visual supports such as ten frames, part part whole and subtraction mats, with the physical objects and resources that can be manipulated.

Pictorial



A group of pictures for children to cross out or cover quantities to support subtraction.



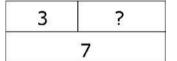
Use visual supports such as ten frames, part part whole and bar model with pictures/icons.

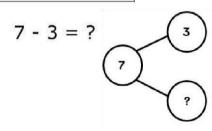
Abstract

A focus on symbols and numbers to form a calculation.



$$10 - 6 = 4$$





* No expectation for children to be able to record a number sentence/addition calculation.

	Subtr	action- Year 1	
Objective and Strategy	Concrete	Pictorial	Abstract
Subtract one-digit and two-digit numbers to 20, including 0. Taking away ones	Use physical objects, counters, cubes etc to show how objects can be taken away. $6-4=2$ $4-2=2$	Cross out drawn objects to show what has been taken away.	7—4 = 3 16—9 = 7
Counting back	Make the larger number in your subtraction. Move the beads along your bead string as you count backwards in ones. 13 - 4 Use counters and move them away from the group as you take ther away counting backwards as you go.	Count back on a number line or track Start at the bigger number and count back the smaller number showing the jumps on the number line.	Put 13 in your head, count back 4. What number are you at? (Use your fingers to help you)

. %

Find the difference			
	Compare objects and amounts 7 'Seven is 3 more than four' 4 'I am 2 years older than my sister' 5 Pencils 3 Erasers Lay objects to represent bar model.	Count on to find the difference. 0 1 2 3 4 5 6 7 8 9 10 11 12 Comparison Bar Models Draw bars to find the difference between 2 numbers. Lisa is 13 years old. Her sister is 22 years old. Find the difference in age between them.	Hannah has 12 sweets and her sister has 5.How many more does Hannah have than her sister?
Represent and use number bonds and related subtraction facts within 20 Part-part whole model	Link to addition. Use PPW model to model the inverse. If 10 is the whole and 6 is one of the arts, what \S the other part? $10-6=4$	Use a pictorial representation of objects to show the part-part whole model	Move to using numbers within the part whole model.
Make 10	Make 14 on the ten frame. Take away the four first to make 10 and then takeaway one more so you have taken away 5. You are left with the answer of 9.	13 - 7 = 6 3 4 5 12 3 4 5 6 7 8 9 10 11 12 13 14 15 16 17 18 19 20 Start at 13. Take away 3 to reach 10. Then take away the remaining 4 so you have taken away 7 altogether. You have reached your answer.	16 – 8= How many do we take off to reach the next 10? How many do we have left to take off?
Vocabulary	equal to, take, take-away, less, minus, subtract, leaves, many left, how much less is	distance between, how many more, how many fewer/	less than, most, least count back, how

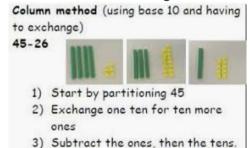
Subtraction- Year 2			
Objective and Strategy	Concrete	Pictorial	Abstract
Subtract a two-digit number and ones, a two-digit number andtens, two two- digit numbers Partitioning to subtract without re-grouping: 'Friendlynumbers'	Use Dienes to show how to partition the number when subtracting without regrouping. The calculation will be shown alongside the manipulative used Model Calculation	Children draw representations of Dienes and cross off. 43—21 = 22	Recording subtraction in columns supports place value and prepares for formal written methods with larger numbers. Toward the end of the year, children move to more formal recording using partitioning method: e.g. 43-21=22 40 and 3 -20 and 1 20 and 2
Make ten strategy	34—28 Use a bead bar or bead strings to model counting to next ten and the rest.	76 80 90 93 'counting on' to find 'difference' Use a number line to count on to next ten and then the rest.	93—76 = 17

left, how much less is...difference, count on, strategy, partition, tens units

	Subtraction- Year 3			
Objective and Strategy	Concrete	Pictorial	Abstract	
To subtract numbers with up to three-digits, using formal written methods of columnar subtraction	47—32	Children are to be secure with use of PV counters before moving onto abstract. Calculations 176 - 64 =	Children should begin with the expanded form. Moving onto a more formal way as below. $47 - 24 = 23$ $728 - 582 = 146$	
Sub traction	Use base 10 or Numicon to model	176 - 64 = 176 - 64 = 112	$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	
Column subtraction (without exchanging)	The calculation will be shown alongside the model chosen to see the connection			
,g.g,	Model Calculation			

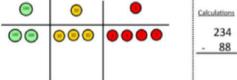
Column
Subtraction
(with
exchanging)

Begin with base 10 or Numicon. Move to pv counters, modelling the exchange of a ten into ten ones. Use the phrase 'take and make' for exchange.

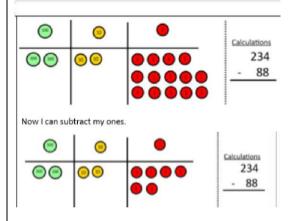


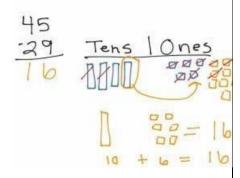
Use Base 10 to start with before moving on to place value counters. Start with one exchange before moving onto subtractions with 2 exchanges.

Make the larger number with the place value counters



Start with the ones, can I take away 8 from 4 easily? I need to exchange one of my tens for ten ones.





When confident, children can find their ownway to record the exchange/regrouping

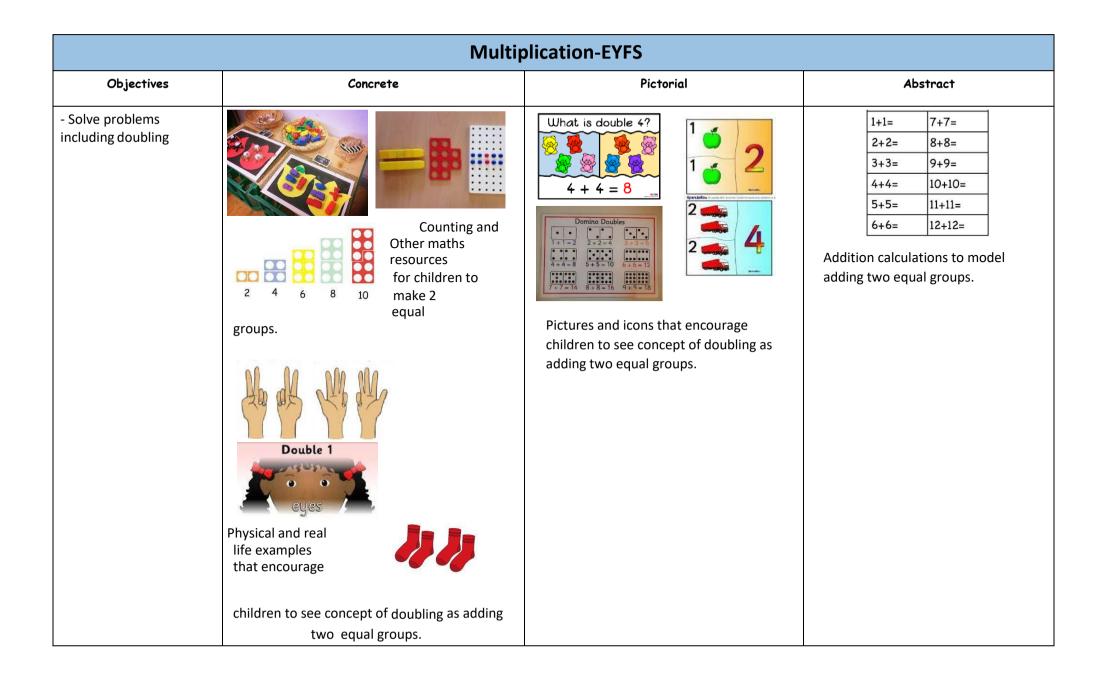
Children should begin with the expanded form. Moving onto a more formal way as below (bottom picture).

	Now look at the tens, can I take away 8 tens easily? I need to exchange one hundred for ten tens.
	© Calculations 234 - 88
	Now I can take away eight tens and complete my subtraction
	© © Calculations 244 - 88 146
	Show children how the concrete method links to the written method alongside your working. Cross out the numbers when exchanging and show where we write our new amount.
Vocabulary	equal to, take, take-away, less, minus, subtract, leaves, distance between, how many more, how many fewer/less than, most, least count back, how many left, how much less isdifference, count on, strategy, partition, tens units

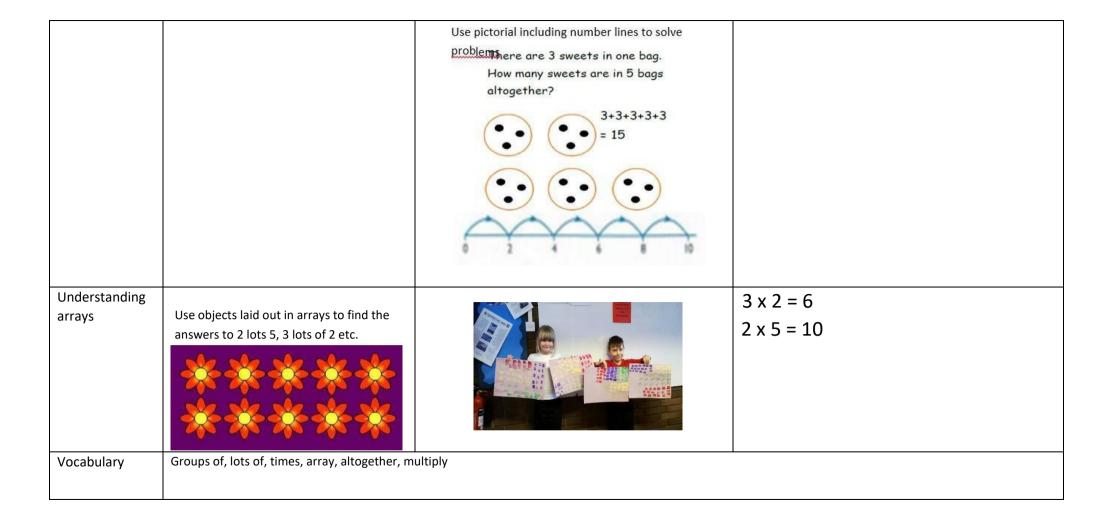
		Subtraction- Year 4	
Objective and Strategy	Concrete	Pictorial	Abstract
Subtract numbers with up to 4 digits using the formal written methods appropriate of columnar subtraction where appropriate Year 4 subtraction with up to 4 digits.	Model process of exchange using Numicon, base ten and then move to PV counters. Use the phrase 'take and make' for exchange- see Y3 The calculation will be shown alongside the model chosen to see the connection Model Calculation	Children to draw pv counters and show their exchange—see Y3 The calculation will be shown alongside the model chosen to see the connection Model Calculation	728-582=146 728-582=146 582 582 146 This will lead to an understanding of subtracting any number including decimals.
Introduce decimal subtraction through context of money	Children to be encouraged to use counters to represent numbers and take counters away to subtract. Ones Tenths Hundredths Thousandths 1 1 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0	52.7 - 27.9 tens ones ten	Rule 2 drop it down! No dward changes the 14 - 15! value! Rule 3 fill 'em in! Think 140 + 6.75 - 7.95 make 15.10 Does at 140 - 7.95 make 15.10 Does at 15.10 make
Vocabulary	equal to, take, take-away, less, minus, subtr many left, how much less isdifference, cou	•	many fewer/less than, most, least count back, how

Subtraction- Year 5/6			
Objective and Strategy	Concrete	Pictorial	Abstract
Subtract with at least 4 digits, including money and measures. Subtract with increasingly large and more complex numbers and decimal values (up to 3 decimal place).	See Year 4	See Year 4	"X" 8 10, 6 9 9 - 89, 9 4 9 - 60, 7 5 0 "Y 10 '5 · 3 4 '1 9 kg - 36 · 08 0 kg - 69 · 33 9 kg
Vocabulary	equal to, take, take-away, less, minus, subtract, leaves, di	_ stance between, how many more, how ma	iny fewer/less than, most, least count back, how many

left, how much less is...difference, count on, strategy, partition, tens units



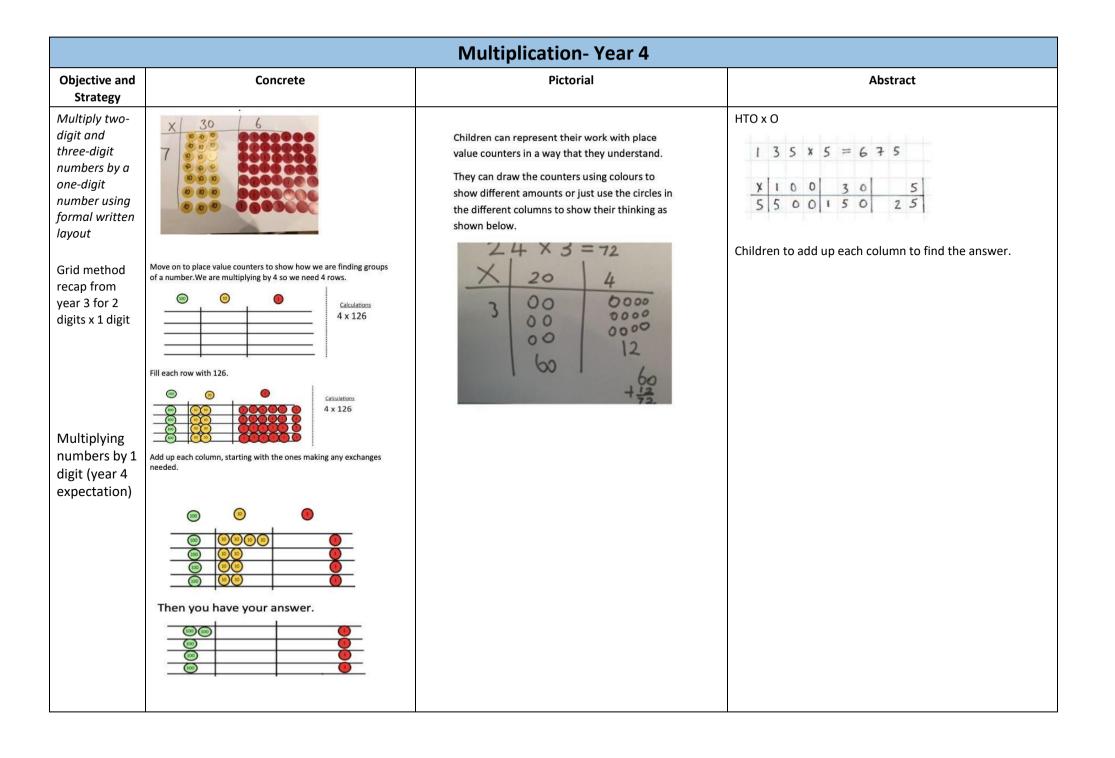
		Multiplication- Year 1	
Objective and	Concrete	Pictorial	Abstract
Strategy Doubling	Use practical activities using manipultives including cubes and Numicon to demonstrate doubling + = = = = = = = = = = = = = = = = = =	Draw pictures to show how to double numbers Double 4 is 8	Partition a number and then double each part before recombining it back together. 10 6
Counting in multiples	Count in multiples supported by concrete objects in equal groups.	Use a number line or pictures to continue support in counting in multiples.	Count in multiples of a number aloud. Write sequences with multiples of numbers. 2, 4, 6, 8, 10 5, 10, 15, 20, 25, 30
Repeated addition	Use different objects to add equal groups.	There are 3 plates. Each plate has 2 star biscuits on. How many biscuits are there? 2 add 2 add 2 equals 6 5 + 5 + 5 = 15	Write addition sentences to describe objects and pictures. $2+2+2+2+2=10$

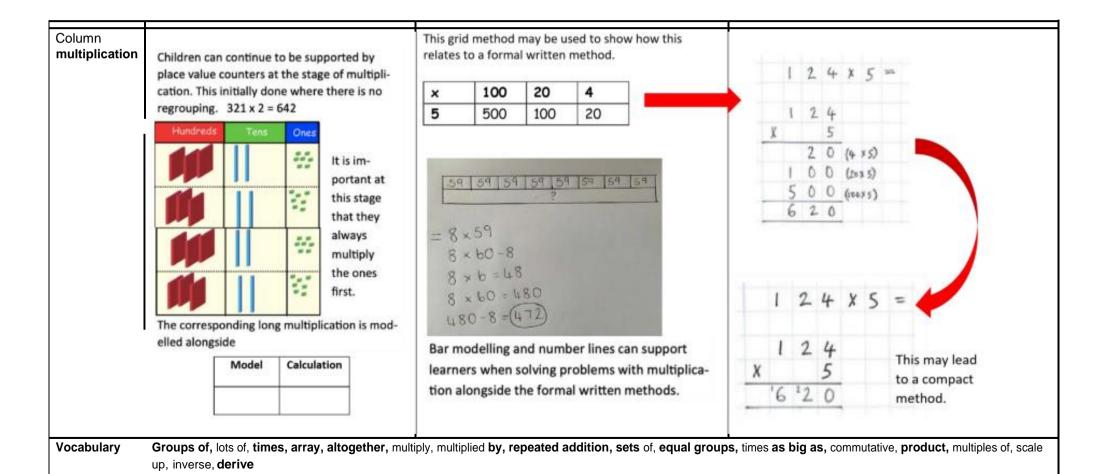


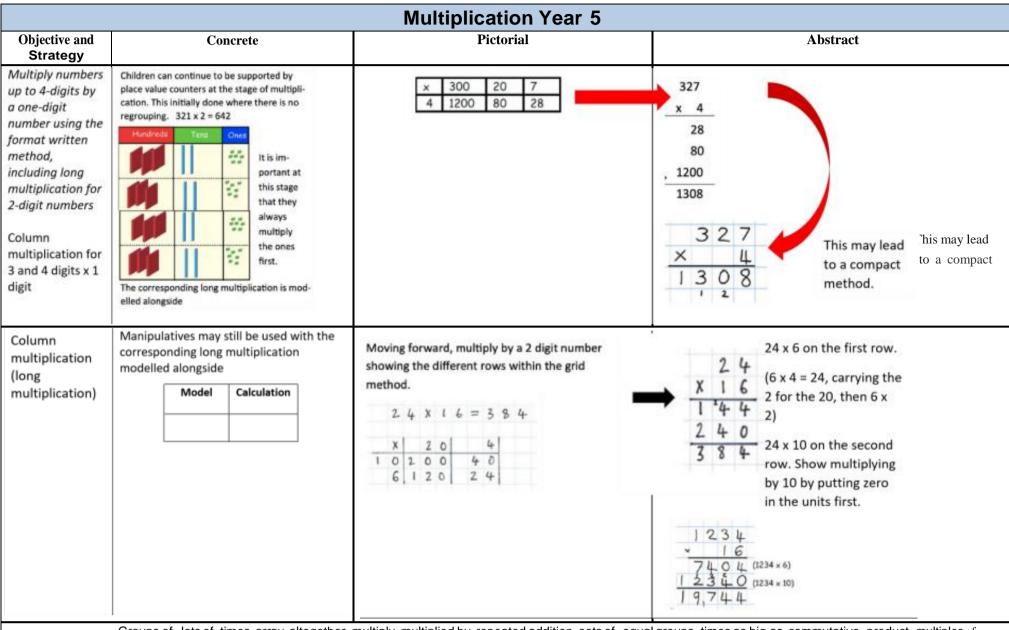
		Multiplication- Year 2	
Objective and Strategy	Concrete	Pictorial	Abstract
Counting in multiples of 2, 3, 4, 5,	Count the groups as children are skip counting, children may use their fingers as they are skip counting. Use bar	Number lines, counting sticks and bar models should be used to show representation of counting in multiples.	Count in multiples of a number aloud.
10 from 0 (repeated addition)	models. 5 + 5 + 5 + 5 + 5 + 5 + 5 + 5 = 40	Sur sur sur sur sur sur	Write sequences with multiples of numbers. 0, 2, 4, 6, 8, 10
		5 10 15 20 25 30	0, 3, 6, 9, 12, 15 0, 5, 10, 15, 20, 25, 30
		3 3 3 3	4 × 3 =
Multiplication is commutative	Create arrays using counters and cubes and Numicon.	Use representations of arrays to show different calculations and explore commutativity.	12 = 3 × 4 12 = 4 × 3 Use an array to write multiplication sentences and reinforce repeated addition.
	Pupils should understand that an array can represent different equations and that, as multiplication is commutative, the order of the multiplication does not affect the answer.	0000	5+5+5=15 3+3+3+3+3=15 5 x 3 = 15 3 x 5 = 15

Using the Inverse This should be taught alongside division, so pupils learn how they work alongside each other. Vocabulary	Groups of, lots of, times, array, altogether, multi	$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	2 x 4 = 8 4 x 2 = 8 8 ÷ 2 = 4 8 ÷ 4 = 2 8 = 2 x 4 8 = 4 x 2 2 = 8 ÷ 4 4 = 8 ÷ 2 Show all 8 related fact family sentences.
,			

		Multiplication- Year 3	
Objective and Strategy	Concrete	Pictorial	Abstract
Multiplying two-digit number by a one digit number	Show the link with arrays to first introduce the grid method. X	Children can represent their work with place value counters in a way that they understand. They can draw the counters using colours to show different amounts or just use the circles in the different columns to show their thinking as shown below.	Start with multiplying by one digit numbers and showing the clear addition alongside the grid. TO x O 1 9 x 3 = 5 4
Grid method progressing to the formal method.	X T U 4 rows of 13	$\frac{24 \times 3 = 72}{\times 20}$ $\frac{20}{30000000000000000000000000000000000$	Children to add up each column to find the answer.
Solving problems including missing number problems, integer scaling problems.	Move on to place value counters to show how we are finding groups of a number.	Bar model are used to explore missing numbers 4 x = 20	
	Add up each column, starting with the ones making any exchanges needed. The calculation will be shown alongside the model chosen to see the connection Model Calculation	20	
Vocabulary		ltiply, multiplied by, repeated addition, sets of, equal grou	ups, times as big as, commutative, product, multiples of, scale







Vocabulary

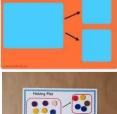
Groups of, lots of, times, array, altogether, multiply, multiplied by, repeated addition, sets of, equal groups, times as big as, commutative, product, multiples of, scale up, inverse, derive, factor pairs, composite numbers, prime number, factors, squared, cubed

Objective and Strategy	Concrete	Pictorial	Abstract
ecimal up to in the units column. Lin		Remind children that the single digit belongs in the units column. Line up the decimal points in the question and the answer.	
			3 · 1 9 × 8 2 5 · 5 2

Division- EYFS			
Objectives	Concrete	Pictorial	Abstract
olve problems including alving and sharing. • Halving a whole, halving a quantity of objects. • Sharing a quantity of objects.	Children have the opportunity to physically cut objects, food or shapes in half.	Pictures and icons that encourage children to see concept of halving in relation to subitising, addition and subtraction knowledge. i.e. Knowing 4 is made of 2 groups of 2, so half of 4 is 2. Bar model with pictures or icons to support understanding of finding 2 equal parts of a number, to further understand how two halves make a whole. Pictures for children to create and visualise 3 or more equal groups.	



Use visual supports such as halving mats and part part whole, with the physical objects and resources that can be manipulated.





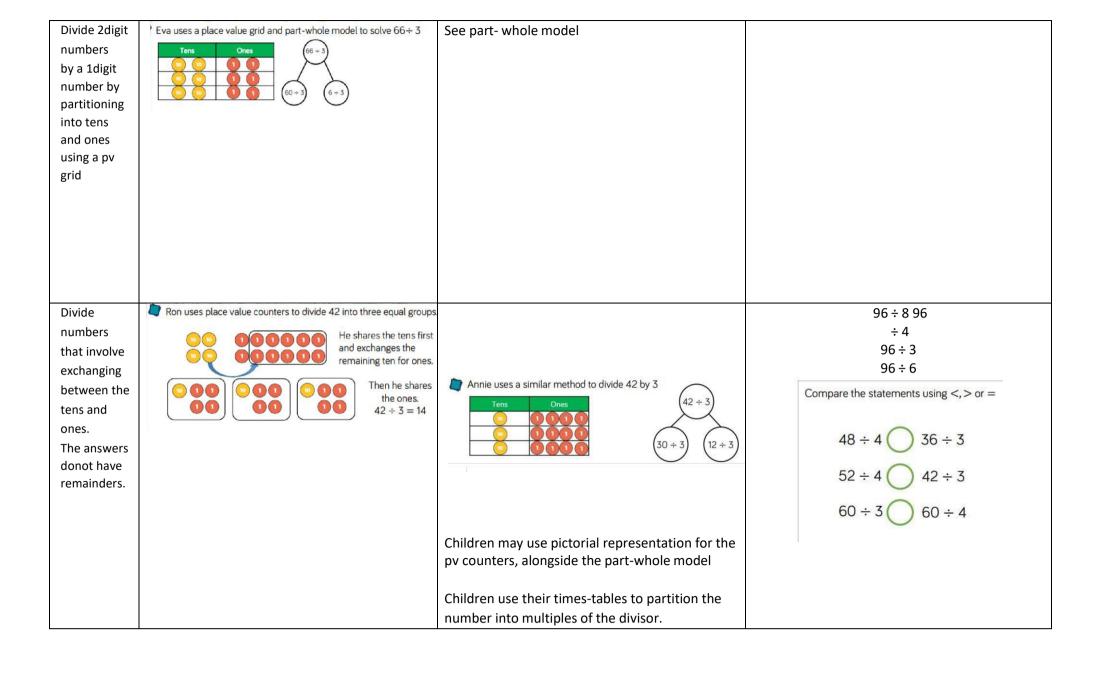
Counting and other maths resources for children to explore sharing between 3 or more.

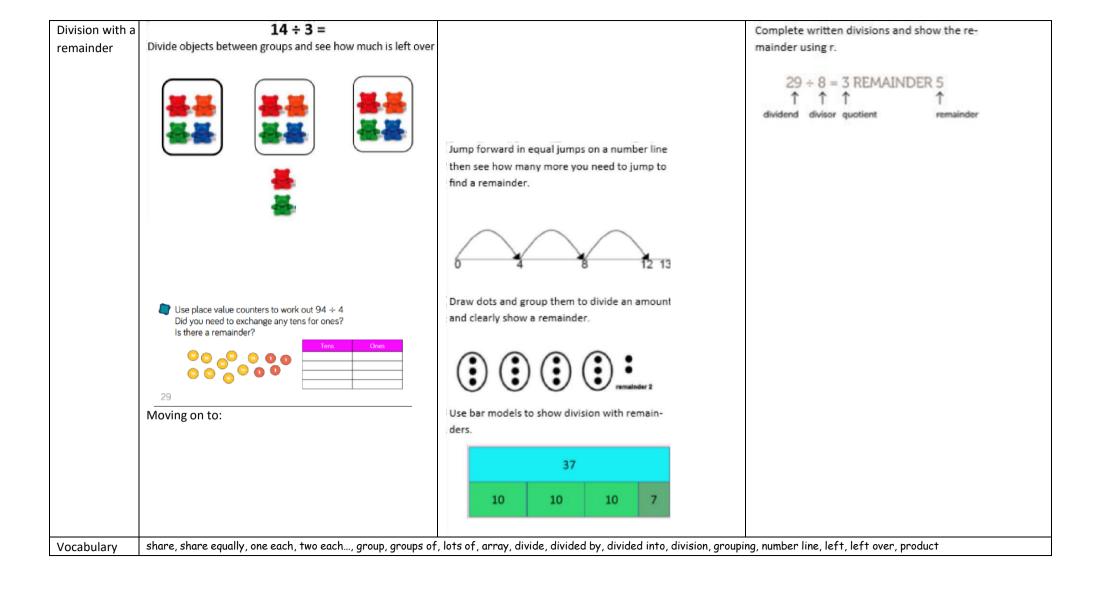
Counting and other maths resources for children to share into two equal groups.

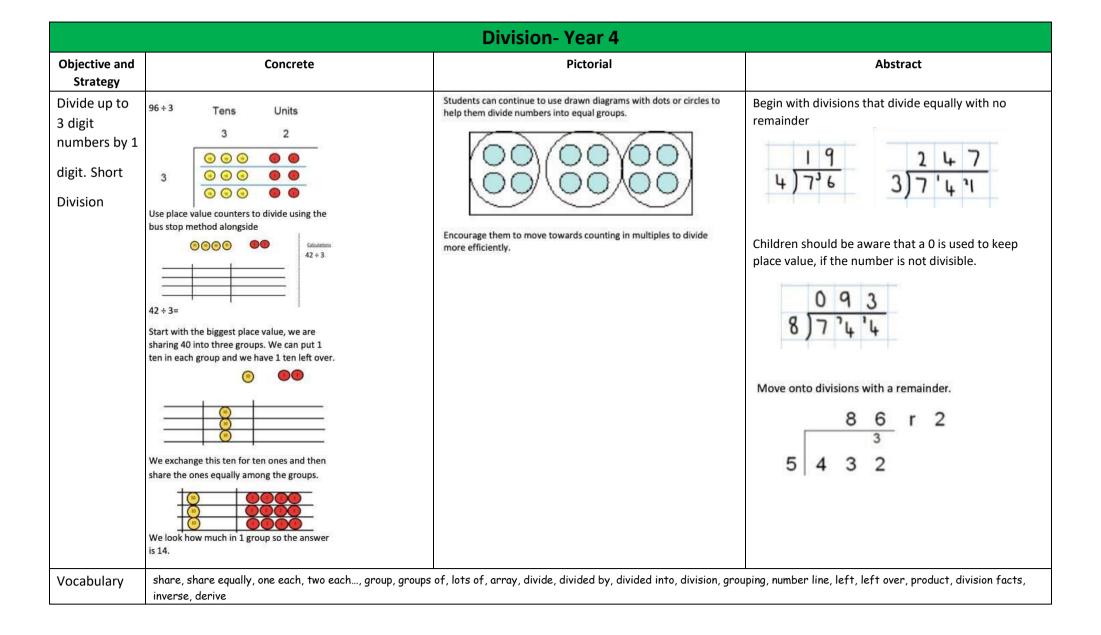
Division- Year 1			
Objective and Strategy	Concrete	Pictorial	Abstract
Division as sharing (sharing objects into groups)	I have 10 cubes, can you share them equally in 2 groups?	Children use pictures or shapes to share quantities. $8 \div 2 = 4$ Children use bar modelling to show and support understanding.	Share 9 buns between three people. 9 ÷ 3 = 3
Vocabulary	share, share equally, one each, two each, group, groups o	of, lots of, array	

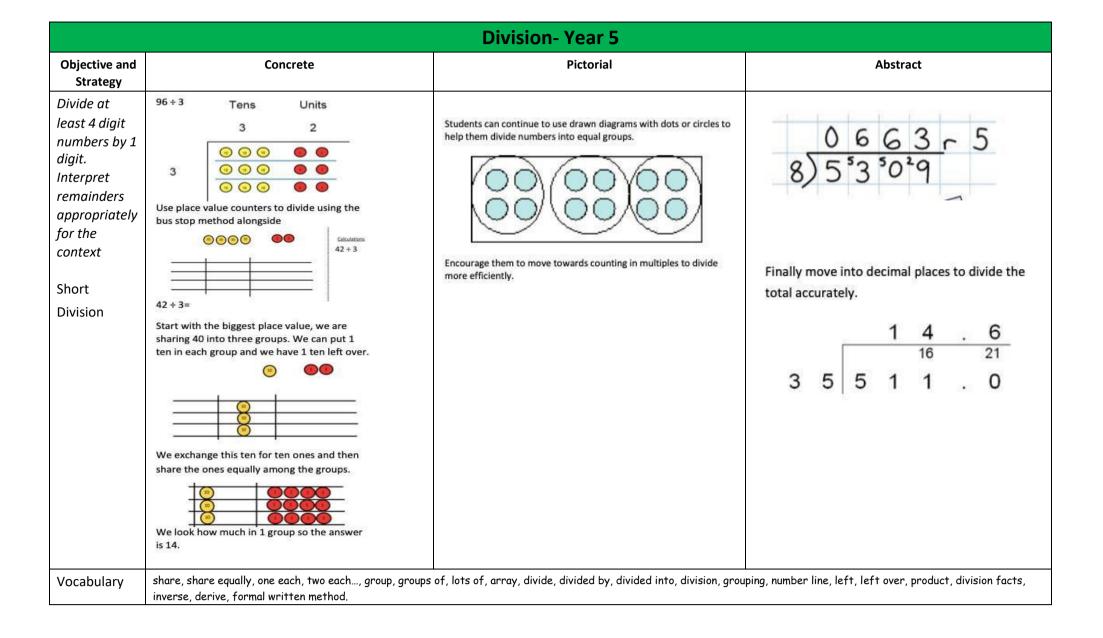
Objective	Concrete	Pictorial	Abstract
and Strategy			
Division as grouping	Divide quantities into equal groups. Use cubes, counters, objects or place value counters to aid understanding. 96 + 3 = 32	Use a number line to show jumps in groups. The number of jumps equals the number of groups. 0 1 2 3 4 5 6 7 8 9 10 11 12	
	0 5 10 15 20 25 30 35	Think of the bar as a whole. Split it into the number of groups you an dividing by and work out how many would be within each group. 20 20 $20 \div 5 = ?$ $5 \times ? = 20$	28 ÷ 7 = 4 Divide 28 into 7 groups. How many are in each group?

		Division- Year 3	
Objective and Strategy	Concrete	Pictorial	Abstract
Division as grouping	Use cubes, counters, objects or place value counters to aid understanding. 24 divided into groups of 6 = 4 96 + 3 = 32	Continue to use bar modelling to aid solving division problems. 20 ? 20 ÷ 5 = ? 5 x ? = 20	How many groups of 6 in 24? 24 ÷ 6 = 4
Division with arrays	Link division to multiplication by creating an array and thinking about the number sentences that can be created. Eg $15 \div 3 = 5$ $5 \times 3 = 15$ $15 \div 5 = 3$ $3 \times 5 = 15$	Draw an array and use lines to split the array into groups to make multiplication and division sentences	Find the inverse of multiplication and division sentences by creating eight linking number sentences. 7 x 4 = 28 4 x 7 = 28 28 ÷ 7 = 4 28 ÷ 4 = 7 28 = 7 x 4 28 = 4 x 7 4 = 28 ÷ 7 7 = 28 ÷ 4









	Division-Year 6	
Objective and Strategy	Abstract	
Long Division	Step 1 – a remainder in the ones	
	0 4 1 R1 4) 16 5	
	4 does not go into 1 (hundred). So combine the 1 hundred with the 6 tens (160).	
	4 goes into 16 four times.	
	4 goes into 5 once, leaving a remainder of 1.	
	8) 32 07	
	8 does not go into 3 of the thousands. So combine the 3 thousands with the 2 hundreds (3,200).	
	8 goes into 32 four times (3,200 + 8 = 400) 8 goes into 0 zero times (tens). 8 goes into 7 zero times, and leaves a remainder of 7. h t o 0 6 1	
	4) 247	
	When dividing the ones, 4 goes into 7 one time. Multiply $1 \times 4 = 4$, write that four under the 7, and subract. This finds us the remainder of 3.	
	Check: 4 × 61 + 3 = 247	
	th h t o	
	0402 4)1609 -8 1	
	When dividing the ones, 4 goes into 9 two times. Multiply $2 \times 4 = 8$, write that eight under the 9, and subract. This finds us the remainder of 1.	
	Check: 4 × 402 + 1 = 1,609	
	Step 2 – a remainder in the tens	

1. Divide.	2. Multiply & subtract.	3. Drop down the next digit.	
2 2)58	2) 5 8	2 9 2) 5 <mark>8</mark>	
Two goes into 5 two times, or 5 tens + 2 = 2 whole tens but there is a remainder!	To find it, multiply 2 × 2 = 4, write that 4 under the five, and subtract to find the remainder of 1 ten.	Next, drop down the 8 of the ones next to the leftover 1 ten. You combine the remainder ten with 8 ones, and get 18.	

1. Divide.	2. Multiply & subtract.	3. Drop down the next digit.	
t o	t o	t o	
2 9 2) 5 8	2 9 2) 5 8	2 2 9 2) 5 8	
<u>-4</u>	<u>- 4</u>	<u>-4</u>	
10	-18	-18	
	0	0	
Divide 2 into 18. Place 9 into the quotient.	Multiply 9 × 2 = 18, write that 18 under the 18, and subtract.	The division is over since there are no more digits in the dividend. The quotient is 29.	

Step 3 – a remainder in any of the place values

1. Divide.	2. Multiply & subtract.	3. Drop down the next digit.
2)278	2)278 =20	1 8 2) 2 7 8 -2 1 0 7
Two goes into 2 one time, or 2 hundreds + 2 = 1 hundred.	Multiply 1 × 2 = 2, write that 2 under the two, and subtract to find the remainder of zero.	Next, drop down the 7 of the tens next to the zero.
Divide.	Multiply & subtract.	Drop down the next digit.
1 3 2) 2 7 8 2 0 7 Divide 2 into 7. Place 3 into the quotient.	h t o 13 2)278 207 6 1 Multiply 3 × 2 = 6, write that 6 under the 7, and subtract to find the remainder of 1 ten.	Next, drop down the 8 of the ones next to the 1 leftover ten.
1. Divide.	2. Multiply & subtract.	3. Drop down the next digit.
1 3 9 2) 2 7 8 2 0 7 6 18 Divide 2 into 18. Place 9 into the quotient.	h t o 1 3 9 2) 2 7 8 -2 0 7 - 6 1 8 -1 8 0 Multiply 9 × 2 = 15, write that 18 under the 18, and subtract to find the remainder of zero.	139 2)278 -207 -618 -18 -180 There are no more digits to drop down. The quotient is 139.

Divide numbers up to 4 digits by a two- digit whole number using the formal written method of division	$ \begin{array}{c cccccccccccccccccccccccccccccccccc$
Vocabulary	share, share equally, one each, two each, group, groups of, lots of, array, divided by, divided into, division, grouping, number line, left, left over, product, division facts, inverse, derive, formal written method.

Minimal Resources required to support the CPA approach (depending on year group):

- 10 frames (including egg boxes)
- Straws/pipe cleaners
- Bead strings (to 20 and 100)
- Base 10/Dienes
- Place value grids
- Double-sided counters
- Part-part whole templates
- Place value counters (KS2)
- Multi-link cubes