

Repton Manor Primary School
Maths Calculation Policy
2025-2026

Including Vocabulary Progression



Repton Manor Primary School Calculation Policy 2025-2026

This policy supports the White Rose maths scheme used throughout the school. Progression within each area of calculation is in line with the programme of study in the 2014 National Curriculum. This calculation policy should be used to support children to develop a deep understanding of number and calculation. This policy has been designed to teach children using concrete, pictorial and abstract representations.

- **Concrete representation**— a child is first introduced to an idea or skill by acting it out with real objects. This is a 'hands on' component using real objects and is a foundation for conceptual understanding.
- **Pictorial representation** - a child has sufficiently understood the 'hands on' experiences performed and can now relate them to representations, such as a diagram or picture of the problem.
- **Abstract representation**—a child is now capable of representing problems by using mathematical notation, for example $12 \times 2 = 24$.

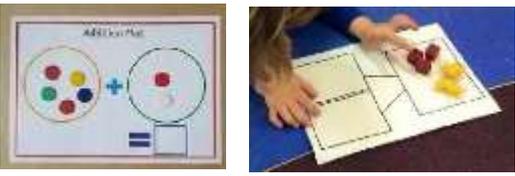
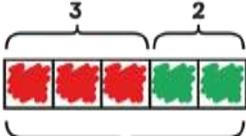
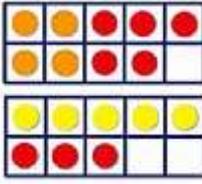
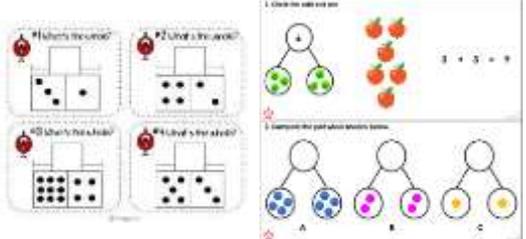
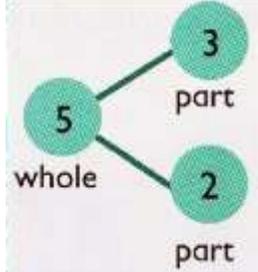
It is important that conceptual understanding, supported by the use of representation, is secure for all procedures. Reinforcement is achieved by going back and forth between these representations.

Mathematics Mastery: At the centre of the mastery approach to the teaching of mathematics is the belief that all children have the potential to succeed. They should have access to the same curriculum content and, rather than being extended with new learning, they should deepen their conceptual understanding by tackling challenging and varied problems. Similarly, with calculation strategies, children must not simply rote learn procedures but demonstrate their understanding of these procedures with concrete materials and pictorial representations. This policy outlines the different calculation strategies that should be taught and used in line with the requirements of the 2014 Primary National Curriculum.

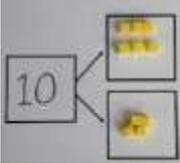
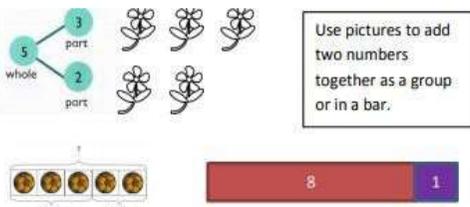
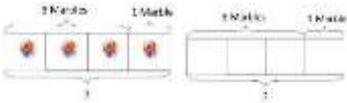
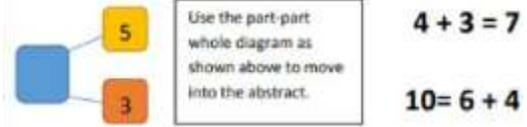
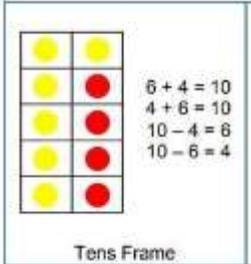
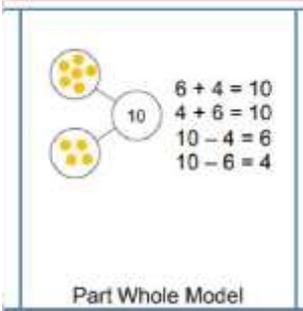
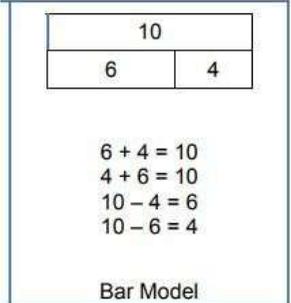
How to use the policy: This mathematics policy is a guide for all staff. All teachers have been given the scheme of work from the White Rose Maths Hub and are required to base their planning around their year group's modules and not to move onto a higher year group's scheme work. These modules use the Singapore Maths Methods and are affiliated to the workings of the 2014 Maths Programme of Study. Teachers can use any teaching resources that they wish to use and the policy does not recommend one set of resources over another, rather that, a variety of resources are used.

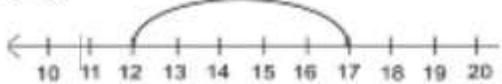
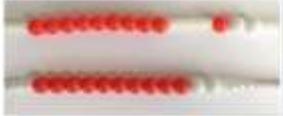
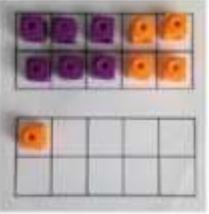
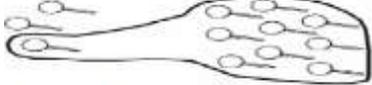
For each of the four number operations, different strategies are laid out, together with examples of what concrete materials can be used and how, along with suggested pictorial representations. The principle of the concrete-pictorial-abstract (CPA) approach [Build it, Draw it, Solve it] is for children to have a true understanding of a mathematical concept, they need to master all three phases within a year group's scheme of work.

Addition - EYFS

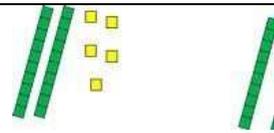
Objectives	Concrete	Pictorial	Abstract																								
<ul style="list-style-type: none"> - Knows that a group of things change in quantity when something is added. - Find the total number of items in two groups by counting all of them. - Says the number that is one more than a given number. - Finds one more from a group of up to five objects, then ten objects. - In practical activities and discussion, beginning to use the vocabulary involved in adding. - Using quantities and objects, they add two single digit numbers and count on to find the answer. - Solve problems including doubling. 	<div style="display: flex; justify-content: space-around;">  </div> <p style="text-align: center;">Use toys and general classroom resources for children to physically manipulate, group/regroup.</p> <div style="display: flex; justify-content: space-around;">  </div> <p style="text-align: center;">Use specific maths resources such as counters, snap cubes, Numicon etc.</p> <div style="display: flex; justify-content: space-around;">  </div> <div style="display: flex; justify-content: space-around;">  </div> <p style="text-align: center;">Use visual supports such as ten frames, part part whole and addition mats, with the physical objects and resources that can be manipulated.</p>	<div style="display: flex; justify-content: space-around;">   </div> <p style="text-align: center;">Two groups of pictures so children are able to count the total.</p> <div style="display: flex; justify-content: center; align-items: center;">  </div> <p style="text-align: center;">Bar model using visuals, pictures/icons or colours.</p> <div style="display: flex; justify-content: center; align-items: center;">  </div> <div style="display: flex; justify-content: center; align-items: center;">  </div> <p style="text-align: center;">Use visual supports such as ten frames, part part whole and addition mats with pictures/icons.</p> <div style="display: flex; justify-content: space-around;">  </div>	<p style="text-align: center;">A focus on symbols and numbers to form a calculation.</p> <div style="text-align: center; border: 1px solid black; padding: 10px; width: fit-content; margin: 0 auto;"> $5 + 2 = 7$ </div> <div style="text-align: center; margin: 10px 0;">  </div> <div style="display: flex; justify-content: space-around; margin-top: 20px;"> <table border="1" style="border-collapse: collapse; text-align: center;"> <tr><td> </td><td> </td></tr> <tr><td>2</td><td>3</td></tr> </table> <table border="1" style="border-collapse: collapse; text-align: center;"> <tr><td> </td><td> </td></tr> <tr><td>4</td><td>5</td></tr> </table> </div> <div style="display: flex; justify-content: space-around; margin-top: 10px;"> <table border="1" style="border-collapse: collapse; text-align: center;"> <tr><td>5</td><td>7</td></tr> <tr><td> </td><td> </td></tr> </table> <table border="1" style="border-collapse: collapse; text-align: center;"> <tr><td>3</td><td>3</td></tr> <tr><td> </td><td> </td></tr> </table> </div> <div style="display: flex; justify-content: space-around; margin-top: 10px;"> <table border="1" style="border-collapse: collapse; text-align: center;"> <tr><td>5</td><td>5</td></tr> <tr><td> </td><td> </td></tr> </table> <table border="1" style="border-collapse: collapse; text-align: center;"> <tr><td>6</td><td> </td></tr> <tr><td>7</td><td> </td></tr> </table> </div> <p style="text-align: center; margin-top: 20px;">* No expectation for children to be able to record a number sentence/addition calculation.</p>			2	3			4	5	5	7			3	3			5	5			6		7	
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Addition- Year 1

Objective and Strategy	Concrete	Pictorial	Abstract
<p>Combining two parts to make a whole: part- whole model</p>	 <p>Use cubes to add two numbers together as a group or in a bar. (Some children may still need to use real objects)</p>  <p>Use part-part whole model</p>	 <p>Use pictures to add two numbers together as a group or in a bar.</p> <p>The <u>Bar Model</u> will be continued from EYFS as a method to support problem solving involving addition, continuing with the concrete representations and moving onto using pictorial representations of objects. Some children will also move onto the abstract.</p>  <p style="text-align: center;">Pictorial (concrete) Abstract</p>	 <p>Use the part-part whole diagram as shown above to move into the abstract.</p> <p style="text-align: right;">$4 + 3 = 7$</p> <p style="text-align: right;">$10 = 6 + 4$</p>
<p>Represent and use number bonds and related subtraction facts within 20</p>	 <p style="text-align: center;">Tens Frame</p> <p>(Some children may need to initially use real objects then move onto the representation, egg boxes may also be used to support this)</p>	 <p style="text-align: center;">Part Whole Model</p>	 <p style="text-align: center;">Bar Model</p> <p>Bar model and part-part whole to be used alongside abstract</p>

<p>Addition and subtraction of one-digit and two-digit numbers to 20 including 0.</p>		<p>$6 + 3 = 9$</p>  <p>Start at the larger number on the number line and count on in ones.</p>	<p>$5 + 12 = 17$ $17 = 12 + 5$</p>
<p>Start at the bigger number and counting on</p>	<p>Start with the larger number on the bead string and then count of to the smaller number 1 by 1 to find the answer.</p>	<p>$12 + 5 = 17$</p>  <p>Start at the larger number on the number line and count on in ones or in one jump to find the answer.</p>	<p>Place the larger number in your head and count on the smaller number to find your answer.</p>
<p>Regrouping to make 10 (The 'Make 10' strategy)</p>	<p>$6 + 5 = 11$</p>   <p>Start with the bigger number and use the smaller number to make 10. Use ten frames.</p>	<p>$3 + 9 =$</p>  <p>Use pictures or a number line. Regroup or Partition the smaller number using the part part whole model to make 10.</p> <p>$9 + 5 = 14$</p> 	<p>$7 + 4 = 11$</p> <p>If I am at seven, how many more do I need to make 10. How many more do I add on now?</p>
<p>Vocabulary</p>	<p>add, more, plus, and, make, altogether, total, equal to, equals, double, most, count on, number line, balancing, part, part, whole</p>		

Adding a 2-digit number and multiples of 10

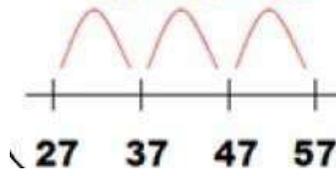


$$25 + 10 = 35$$

Explore that the ones digit does not change

$$27 + 30$$

$$+10 \quad +10 \quad +10$$



Base 10 may be used above the number line initially.
The calculation will be shown alongside the number line to see the connection

$$27 + 10 = 37$$

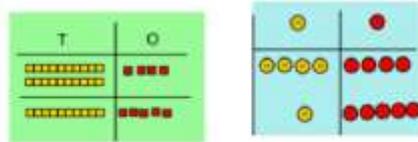
$$27 + 20 = 47$$

$$27 + \square = 57$$

Adding two 2-digit numbers (No re-grouping)

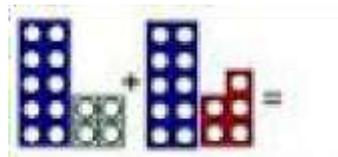
$$24 + 15 =$$

Add together the ones first then add the tens. Use the Base 10 blocks first before moving onto place value counters.



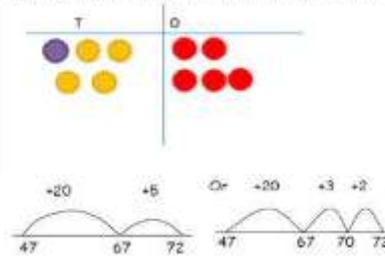
(Some children may not be ready for place value counters in Y2)

Numicon be used



may also

After practically using the base 10 blocks and place value counters, children can draw the counters to help them to solve additions.

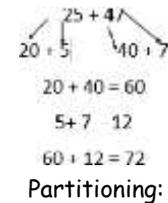


Use number line and bridge ten using part whole if necessary.
Base 10 may be used above the number line.

The calculation will be shown alongside the number line to see the connection

Model	Calculation

The Bar Model (Singapore maths) will be used to support problem solving moving onto the generalisation that $b+c=a$. Children will focus on using the abstract representation with the pictorial to support where necessary.



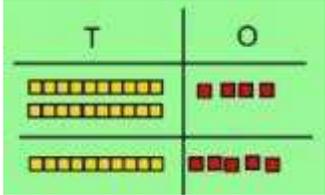
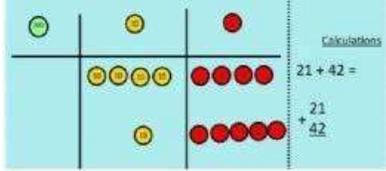
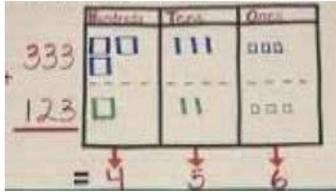
Recording addition in columns supports place value and prepares for formal written methods with larger numbers.
Toward the end of the year, children move to more formal recording using partitioning method:

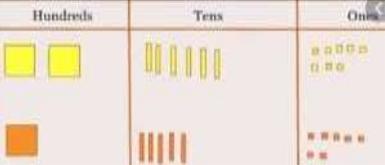
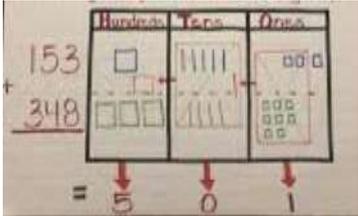
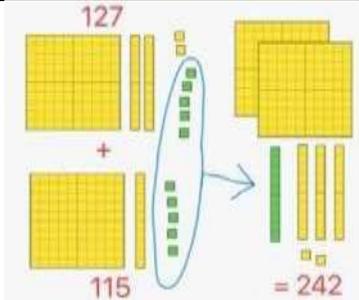
$$\begin{array}{r} 40 + 7 \\ 30 + 5 \\ \hline 70 + 12 \end{array}$$

Vocabulary

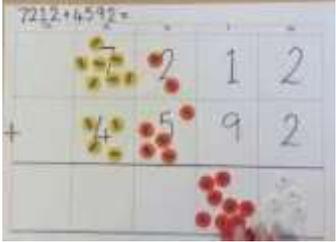
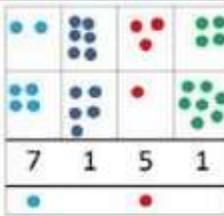
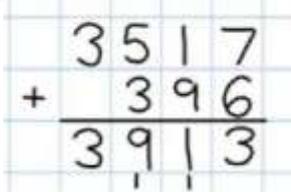
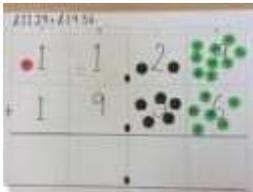
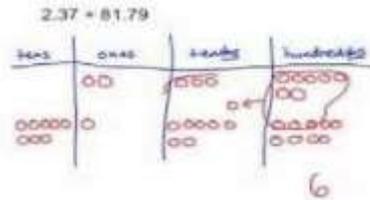
add, more, plus, and, make, altogether, total, equal to, equals, double, most, count on, number line, sum, tens, units, partition, addition, column, tens boundary

Addition- Year 3

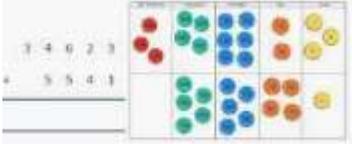
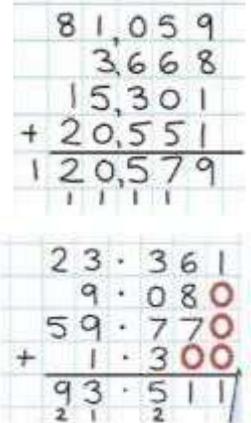
Objective and Strategy	Concrete	Pictorial	Abstract								
<p>Add and subtract numbers with up to 3-digits, using formal written methods of columnar addition</p> <p>Column addition (no regrouping)</p>	<div style="text-align: center;">  </div> <p>Using manipulatives (dienes, numicon, counters), children are to line up hundreds, tens and ones.</p> <div style="text-align: center;">  </div> <p>Children should be secure with using PV counters before moving onto pictorial.</p> <p>The calculation will be shown alongside the model used to see the connection</p> <table border="1" style="margin-left: auto; margin-right: auto; border-collapse: collapse; text-align: center;"> <thead> <tr> <th style="padding: 2px 10px;">Model</th> <th style="padding: 2px 10px;">Calculation</th> </tr> </thead> <tbody> <tr> <td style="height: 40px;"></td> <td></td> </tr> </tbody> </table>	Model	Calculation			<div style="text-align: center;">  </div> <p>Children are to draw, in a PV frame, the manipulatives, that they are using.</p> <p>Secure knowledge of representation with the PV columns.</p> <p>The calculation will be shown alongside the model to see the connection</p> <table border="1" style="margin-left: auto; margin-right: auto; border-collapse: collapse; text-align: center;"> <thead> <tr> <th style="padding: 2px 10px;">Model</th> <th style="padding: 2px 10px;">Calculation</th> </tr> </thead> <tbody> <tr> <td style="height: 40px;"></td> <td></td> </tr> </tbody> </table>	Model	Calculation			<div style="text-align: center;"> $\begin{array}{r} 223 \\ + 114 \\ \hline 337 \end{array}$ </div> <p>Children to move onto recording more formally.</p> <p>Some children may need to use the expanded method (see below).</p>
Model	Calculation										
Model	Calculation										

<p>Column addition (with regrouping)</p>		 <p>Children can draw a representation of the grid to further support their understanding, carrying the ten underneath the line.</p>	$\begin{array}{r} 20 + 5 \\ 40 + 8 \\ \hline 60 + 13 = 73 \end{array}$ <p>Children are to begin with the abstract: expanded form. For those children, that are confident after AFL, the below method should be used.</p>
	 <p>Exchange ten ones for a ten. Model using Dienes, Numicon and place value counters.</p>		$\begin{array}{r} 536 \\ + 85 \\ \hline 621 \\ 11 \end{array}$
<p>Vocabulary</p>	<p>addition add, more, and make, sum, total, altogether, double, near double, half, halve, tens boundary, hundreds boundary</p>		

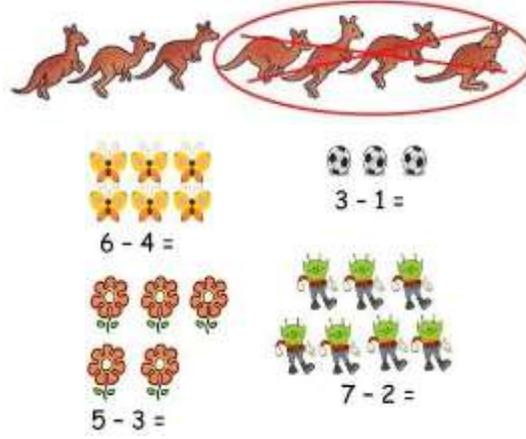
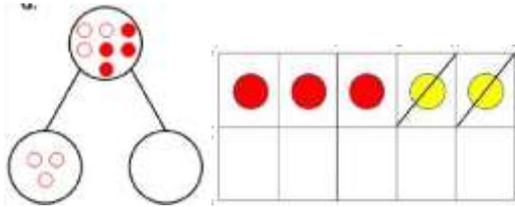
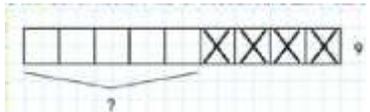
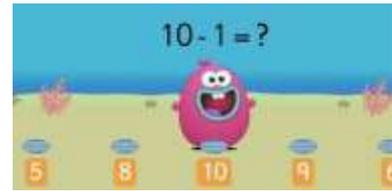
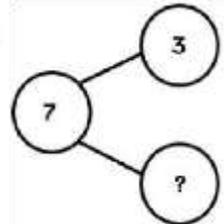
Addition- Year 4

Objective and Strategy	Concrete	Pictorial	Abstract				
<p><i>Using formal written methods of columnar addition where appropriate</i></p> <p>add numbers with up to 4 digits (with exchange)</p>	<p>Children continue to use dienes or place value counters to add, exchanging ten ones for a ten and ten tens for a hundred and ten hundreds for a thousand.</p>  <p style="text-align: center;">The calculation will be shown alongside the manipulative used to see the connection</p> <table style="margin-left: auto; margin-right: auto; border-collapse: collapse;"> <thead> <tr> <th style="border: none; padding: 5px;">Model</th> <th style="border: none; padding: 5px;">Calculation</th> </tr> </thead> <tbody> <tr> <td style="border: 1px solid black; width: 50px; height: 40px;"></td> <td style="border: 1px solid black; width: 50px; height: 40px;"></td> </tr> </tbody> </table>	Model	Calculation			 <p style="text-align: center;">Children can draw a pictorial representation of the columns and place value counters to further support their learning and understanding.</p>	 <p style="text-align: center;">Continue from previous work to carry hundreds as well as tens.</p>
Model	Calculation						
<p>Add decimals with 2 decimal places, including money.</p>	 <p style="text-align: center;">Introduce decimal place value counters and model exchange for addition.</p>		 <p style="text-align: center;">As the children move on, introduce decimals with the same number of decimal places and different. Money can be used here.</p>				
<p>Vocabulary</p>	<p>addition add, more, and make, sum, total, altogether, double, near double, half, halve, tens boundary, hundreds boundary, decimal, decimal point</p>						

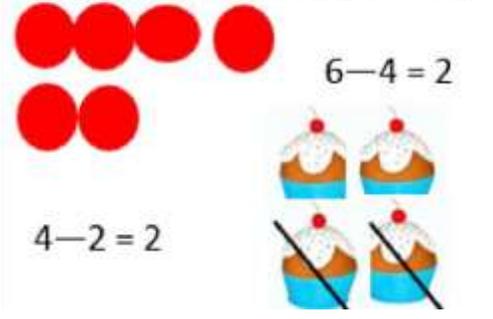
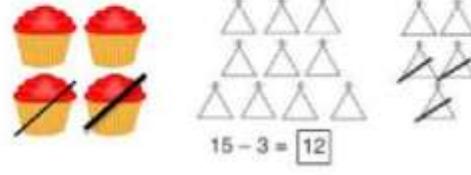
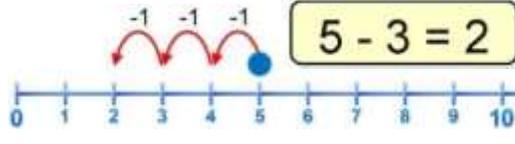
Addition- Year 5/6

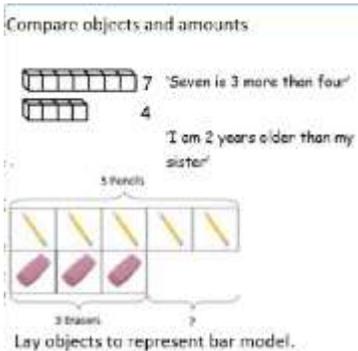
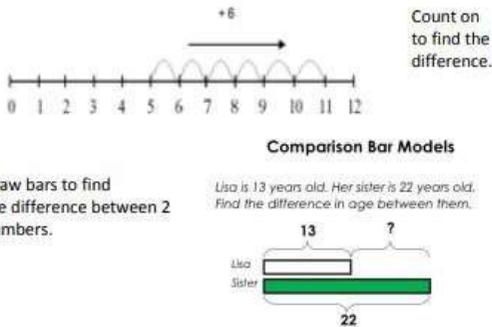
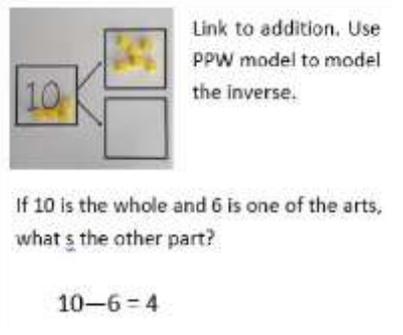
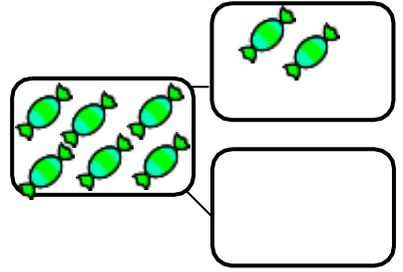
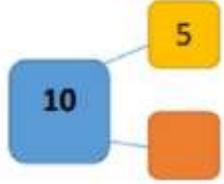
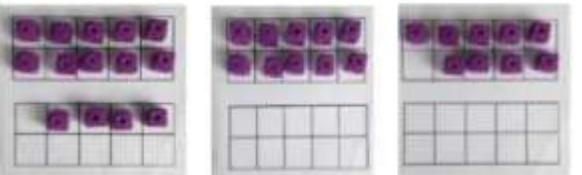
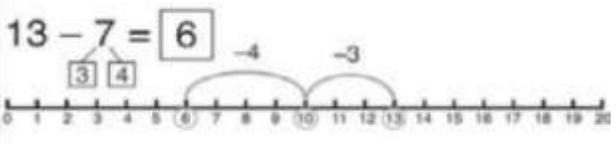
Objective and Strategy	Concrete	Pictorial	Abstract
add numbers with more than 4 digits.	See Year 4	See Year 4	<div style="text-align: center;">  </div> <p style="text-align: center;">Children should have abstract supported by a pictorial or concrete if needed.</p>
add several numbers of increasing complexity, including adding money, measure and decimals with different numbers of decimal points.	See Year 4	See Year 4	<div style="text-align: center;">  </div> <p style="text-align: center;">Insert zeros for place holders.</p>
Vocabulary	addition add, more, and make, sum, total, altogether, double, near double, half, halve, tens boundary, hundreds boundary, decimal, decimal point		

Subtraction- EYFS

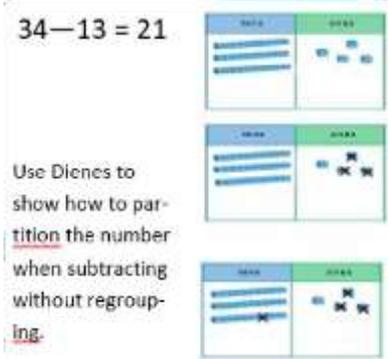
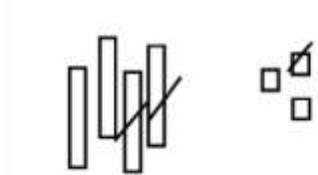
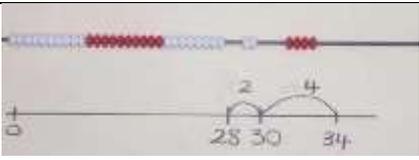
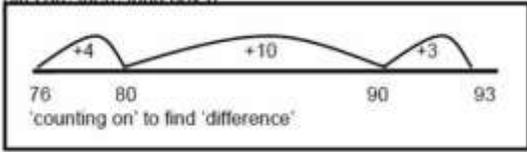
Objectives	Concrete	Pictorial	Abstract				
<ul style="list-style-type: none"> - Knows that a group of things change in quantity when something is taken away - Find one less from a group of five objects, then ten objects. - In practical activities and discussion, beginning to use the vocabulary involved in subtracting. - Using quantities and objects, they subtract two single digit numbers and count back to find the answer. 	 <p>Use toys and general classroom resources for children to physically manipulate, group/regroup.</p>    <p>Use specific maths resources such as snap cubes, Numicon, bead strings etc.</p>   <p>Use visual supports such as ten frames, part part whole and subtraction mats, with the physical objects and resources that can be manipulated.</p>	 <p>A group of pictures for children to cross out or cover quantities to support subtraction.</p>   <p>Use visual supports such as ten frames, part part whole and bar model with pictures/icons.</p>	<p>A focus on symbols and numbers to form a calculation.</p>  <div style="border: 2px solid blue; padding: 5px; display: inline-block; margin: 10px;"> $10 - 6 = 4$ </div> <table border="1" style="margin: 10px;"> <tr> <td style="width: 50px; text-align: center;">3</td> <td style="width: 50px; text-align: center;">?</td> </tr> <tr> <td colspan="2" style="text-align: center;">7</td> </tr> </table> <p style="margin: 10px;">$7 - 3 = ?$</p>  <p>* No expectation for children to be able to record a number sentence/addition calculation.</p>	3	?	7	
3	?						
7							

Subtraction- Year 1

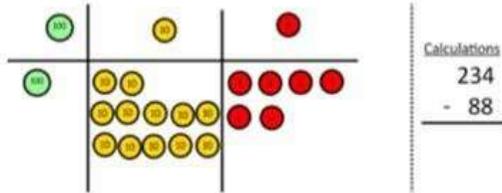
Objective and Strategy	Concrete	Pictorial	Abstract
<p>Subtract one-digit and two-digit numbers to 20, including 0.</p> <p>Taking away ones</p>	<p>Use physical objects, counters, cubes etc to show how objects can be taken away.</p>  <p>$6 - 4 = 2$</p> <p>$4 - 2 = 2$</p>	<p>Cross out drawn objects to show what has been taken away.</p>  <p>$15 - 3 = 12$</p>	<p>$7 - 4 = 3$</p> <p>$16 - 9 = 7$</p>
<p>Counting back</p>	<p>Make the larger number in your subtraction. Move the beads along your bead string as you count backwards in ones.</p> <p>$13 - 4$</p>  <p>Use counters and move them away from the group as you take them away counting backwards as you go.</p> 	 <p>Count back on a number line or track Start at the bigger number and count back the smaller number showing the jumps on the number line.</p>	<p>Put 13 in your head, count back 4. What number are you at? (Use your fingers to help you)</p>

<p>Find the difference</p>	<p>Compare objects and amounts</p>  <p>Lay objects to represent bar model.</p>	 <p>Draw bars to find the difference between 2 numbers.</p> <p>Use a pictorial representation of objects to show the part-part whole model</p>	<p>Hannah has 12 sweets and her sister has 5. How many more does Hannah have than her sister?</p>
<p>Represent and use number bonds and related subtraction facts within 20</p> <p>Part-part whole model</p>	 <p>Link to addition. Use PPW model to model the inverse.</p> <p>If 10 is the whole and 6 is one of the parts, what is the other part?</p> <p>$10 - 6 = 4$</p>	 <p>Use a pictorial representation of objects to show the part-part whole model</p>	 <p>Move to using numbers within the part whole model.</p>
<p>Make 10</p>	<p>$14 - 9 =$</p>  <p>Make 14 on the ten frame. Take away the four first to make 10 and then take away one more so you have taken away 5. You are left with the answer of 9.</p>	<p>$13 - 7 = 6$</p>  <p>Start at 13. Take away 3 to reach 10. Then take away the remaining 4 so you have taken away 7 altogether. You have reached your answer.</p>	<p>$16 - 8 =$</p> <p>How many do we take off to reach the next 10? How many do we have left to take off?</p>
<p>Vocabulary</p>	<p>equal to, take, take-away, less, minus, subtract, leaves, distance between, how many more, how many fewer/less than, most, least count back, how many left, how much less is...</p>		

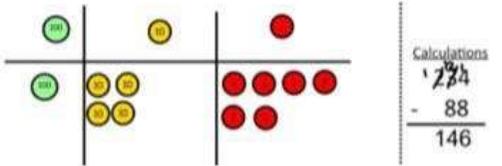
Subtraction- Year 2

Objective and Strategy	Concrete	Pictorial	Abstract				
<p><i>Subtract a two-digit number and ones, a two-digit number and tens, two two-digit numbers</i></p> <p>Partitioning to subtract without re-grouping: 'Friendly numbers'</p>	<p>$34 - 13 = 21$</p>  <p>Use Dienes to show how to partition the number when subtracting without regrouping.</p> <p>The calculation will be shown alongside the manipulative used</p> <table border="1" style="margin-left: auto; margin-right: auto;"> <thead> <tr> <th>Model</th> <th>Calculation</th> </tr> </thead> <tbody> <tr> <td style="height: 30px;"></td> <td></td> </tr> </tbody> </table>	Model	Calculation			<p>Children draw representations of Dienes and cross off.</p>  <p>$43 - 21 = 22$</p>	<p>$43 - 21 = 22$</p> <p><i>Recording subtraction in columns supports place value and prepares for formal written methods with larger numbers.</i></p> <p>Toward the end of the year, children move to more formal recording using partitioning method:</p> <p>e.g. $43 - 21 = 22$</p> <p style="margin-left: 20px;">40 and 3 -20 and 1 <u>20 and 2</u></p>
Model	Calculation						
<p>Make ten strategy</p>	 <p>$34 - 28$</p> <p>Use a bead bar or bead strings to model counting to next ten and the rest.</p>	 <p>Use a number line to count on to next ten and then the rest.</p>	<p>$93 - 76 = 17$</p>				
<p>Vocabulary</p>	<p>equal to, take, take-away, less, minus, subtract, leaves, distance between, how many more, how many fewer/less than, most, least count back, how many left, how much less is...difference, count on, strategy, partition, tens units</p>						

Now look at the tens, can I take away 8 tens easily? I need to exchange one hundred for ten tens.



Now I can take away eight tens and complete my subtraction

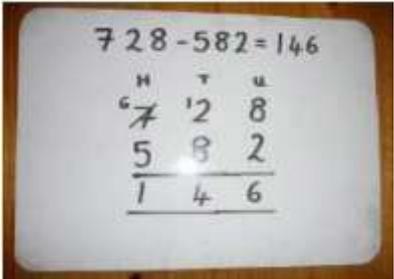
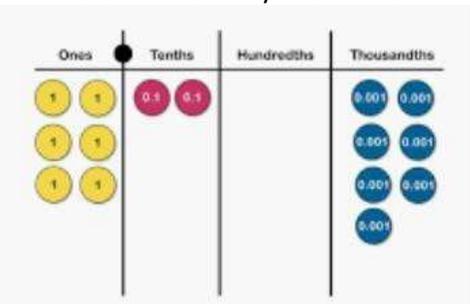
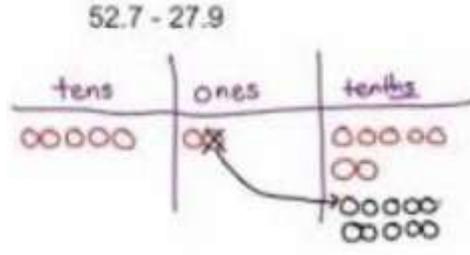
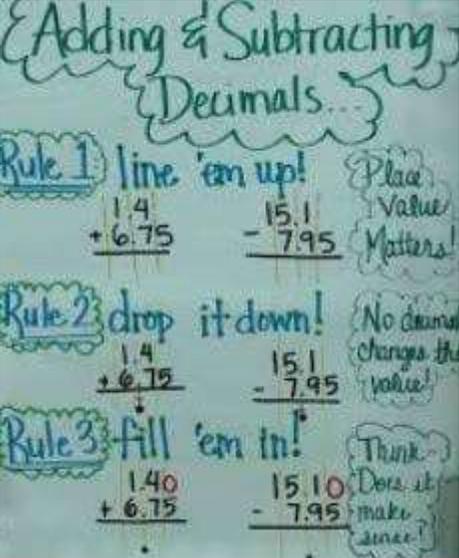


Show children how the concrete method links to the written method alongside your working. Cross out the numbers when exchanging and show where we write our new amount.

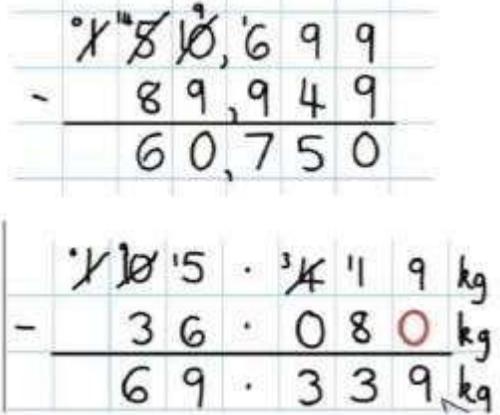
Vocabulary

equal to, take, take-away, less, minus, subtract, leaves, distance between, how many more, how many fewer/less than, most, least count back, how many left, how much less is...difference, count on, strategy, partition, tens units

Subtraction- Year 4

Objective and Strategy	Concrete	Pictorial	Abstract								
<p>Subtract numbers with up to 4 digits using the formal written methods appropriate of columnar subtraction where appropriate</p> <p>Year 4 subtraction with up to 4 digits.</p>	<p>Model process of exchange using Numicon, base ten and then move to PV counters.</p> <p>Use the phrase 'take and make' for exchange- see Y3</p> <p>The calculation will be shown alongside the model chosen to see the connection</p> <div style="text-align: center; margin-top: 20px;"> <table border="1" style="margin: auto;"> <tr> <th style="padding: 5px;">Model</th> <th style="padding: 5px;">Calculation</th> </tr> <tr> <td style="height: 30px;"></td> <td></td> </tr> </table> </div>	Model	Calculation			<p>Children to draw pv counters and show their exchange—see Y3</p> <p>The calculation will be shown alongside the model chosen to see the connection</p> <div style="text-align: center; margin-top: 20px;"> <table border="1" style="margin: auto;"> <tr> <th style="padding: 5px;">Model</th> <th style="padding: 5px;">Calculation</th> </tr> <tr> <td style="height: 30px;"></td> <td></td> </tr> </table> </div>	Model	Calculation			<div style="text-align: center;">  </div> <p style="text-align: center; margin-top: 10px;">This will lead to an understanding of subtracting any number including decimals.</p>
Model	Calculation										
Model	Calculation										
<p>Introduce decimal subtraction through context of money</p>	<p>Children to be encouraged to use counters to represent numbers and take counters away to subtract.</p> <div style="text-align: center; margin-top: 10px;">  </div>	<div style="text-align: center; margin-top: 10px;">  </div> <p style="text-align: center; margin-top: 10px;">When confident, children can find their own way to record the exchange/regrouping</p>	<div style="text-align: center; margin-top: 10px;">  </div>								
<p>Vocabulary</p>	<p>equal to, take, take-away, less, minus, subtract, leaves, distance between, how many more, how many fewer/less than, most, least count back, how many left, how much less is...difference, count on, strategy, partition, tens units</p>										

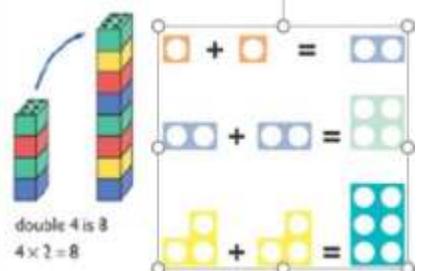
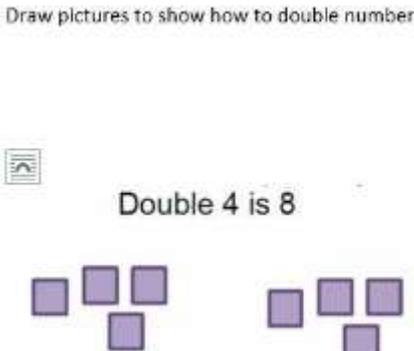
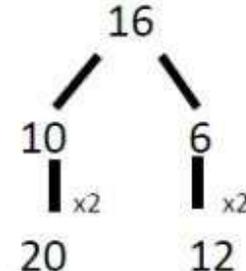
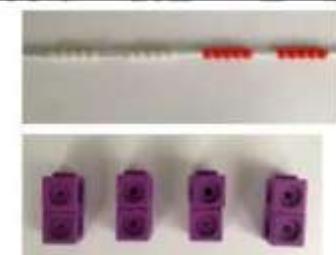
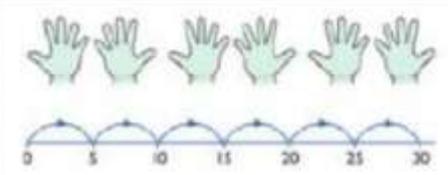
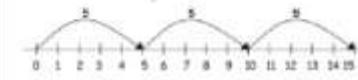
Subtraction- Year 5/6

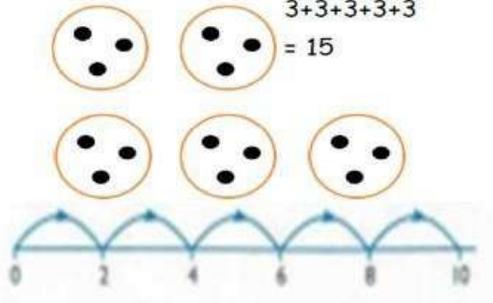
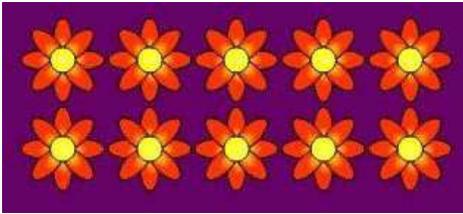
Objective and Strategy	Concrete	Pictorial	Abstract
<p>Subtract with at least 4 digits, including money and measures.</p> <p>Subtract with increasingly large and more complex numbers and decimal values (up to 3 decimal place).</p>	<p>See Year 4</p>	<p>See Year 4</p>	 <p>Handwritten abstract subtraction problems on a grid:</p> $\begin{array}{r} \cancel{8}^{\circ} \cancel{9}^{\circ} \cancel{0}^{\circ}, 699 \\ - \quad 29,199 \\ \hline 60,750 \end{array}$ $\begin{array}{r} \cancel{5}^{\circ} \cancel{0}^{\circ} 5 \cdot \cancel{4}^{\circ} 19 \text{ kg} \\ - \quad 36 \cdot 08 \text{ kg} \\ \hline 69 \cdot 339 \text{ kg} \end{array}$ <p>(Note: The 0 in 3.080 kg is circled in red in the original image.)</p>
<p>Vocabulary</p>	<p>equal to, take, take-away, less, minus, subtract, leaves, distance between, how many more, how many fewer/less than, most, least count back, how many left, how much less is...difference, count on, strategy, partition, tens units</p>		

Multiplication-EYFS

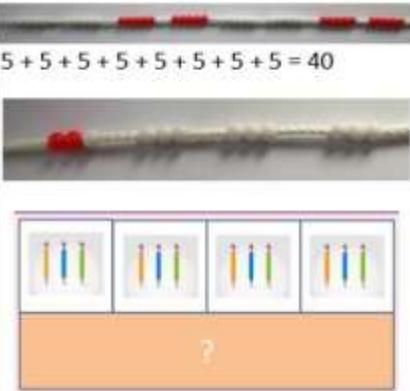
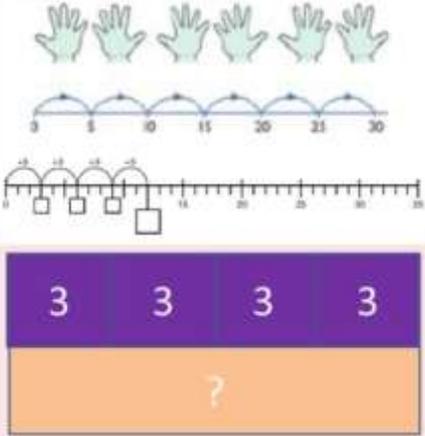
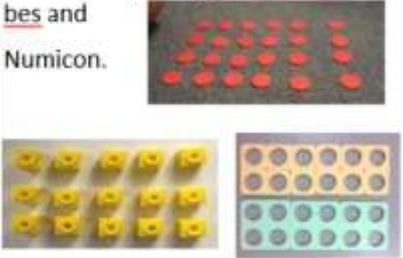
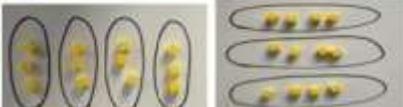
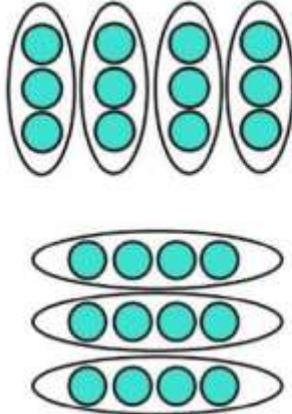
Objectives	Concrete	Pictorial	Abstract												
<p>- Solve problems including doubling</p>	<div data-bbox="465 274 1025 486"> </div> <div data-bbox="481 494 772 662"> <p>Counting and Other maths resources for children to make 2 equal groups.</p> </div> <div data-bbox="481 694 571 726"> <p>groups.</p> </div> <div data-bbox="481 774 795 933"> </div> <div data-bbox="481 941 772 1093"> </div> <div data-bbox="465 1109 672 1204"> <p>Physical and real life examples that encourage</p> </div> <div data-bbox="795 1101 974 1204"> </div> <div data-bbox="481 1268 1019 1340"> <p>children to see concept of doubling as adding two equal groups.</p> </div>	<div data-bbox="1086 279 1332 454"> </div> <div data-bbox="1086 470 1332 662"> </div> <div data-bbox="1377 287 1556 446"> </div> <div data-bbox="1377 454 1556 614"> </div> <p>Pictures and icons that encourage children to see concept of doubling as adding two equal groups.</p>	<table border="1" data-bbox="1747 279 1982 526"> <tbody> <tr> <td>1+1=</td> <td>7+7=</td> </tr> <tr> <td>2+2=</td> <td>8+8=</td> </tr> <tr> <td>3+3=</td> <td>9+9=</td> </tr> <tr> <td>4+4=</td> <td>10+10=</td> </tr> <tr> <td>5+5=</td> <td>11+11=</td> </tr> <tr> <td>6+6=</td> <td>12+12=</td> </tr> </tbody> </table> <p>Addition calculations to model adding two equal groups.</p>	1+1=	7+7=	2+2=	8+8=	3+3=	9+9=	4+4=	10+10=	5+5=	11+11=	6+6=	12+12=
1+1=	7+7=														
2+2=	8+8=														
3+3=	9+9=														
4+4=	10+10=														
5+5=	11+11=														
6+6=	12+12=														

Multiplication- Year 1

Objective and Strategy	Concrete	Pictorial	Abstract
Doubling	<p>Use practical activities using <u>manipulatives</u> including cubes and Numicon to demonstrate doubling</p>  <p>double 4 is 8 $4 \times 2 = 8$</p>	<p>Draw pictures to show how to double numbers</p>  <p>Double 4 is 8</p>	<p>Partition a number and then double each part before recombining it back together.</p>  <p>16</p> <p>10 $\times 2$ 20</p> <p>6 $\times 2$ 12</p>
Counting in multiples	 <p>Count in multiples supported by concrete objects in equal groups.</p>	 <p>Use a number line or pictures to continue support in counting in multiples.</p>	<p>Count in multiples of a number aloud.</p> <p>Write sequences with multiples of numbers.</p> <p>2, 4, 6, 8, 10</p> <p>5, 10, 15, 20, 25, 30</p>
Repeated addition	 <p>Use different objects to add equal groups.</p>	<p>There are 3 plates. Each plate has 2 star biscuits on. How many biscuits are there?</p>  <p>$2 \text{ add } 2 \text{ add } 2 \text{ equals } 6$</p>  <p>$5 + 5 + 5 = 15$</p>	<p>Write addition sentences to describe objects and pictures.</p>  <p>$2 + 2 + 2 + 2 + 2 = 10$</p>

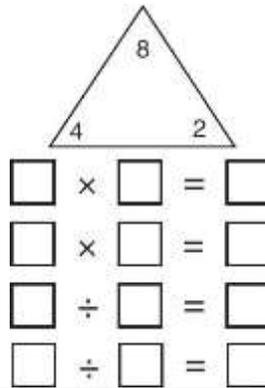
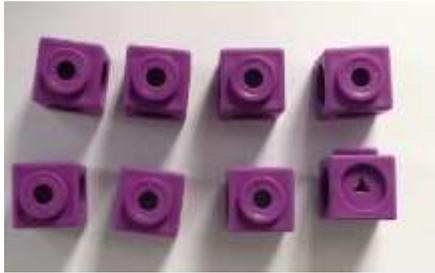
		<p>Use pictorial including number lines to solve problems.</p> <p>There are 3 sweets in one bag. How many sweets are in 5 bags altogether?</p> <p>$3+3+3+3+3 = 15$</p> 	
<p>Understanding arrays</p>	<p>Use objects laid out in arrays to find the answers to 2 lots 5, 3 lots of 2 etc.</p> 		<p>$3 \times 2 = 6$ $2 \times 5 = 10$</p>
<p>Vocabulary</p>	<p>Groups of, lots of, times, array, altogether, multiply</p>		

Multiplication- Year 2

Objective and Strategy	Concrete	Pictorial	Abstract
<p>Counting in multiples of 2, 3, 4, 5, 10 from 0 (repeated addition)</p>	<p>Count the groups as children are skip counting, children may use their fingers as they are skip counting. Use bar models.</p>  <p>$5 + 5 + 5 + 5 + 5 + 5 + 5 + 5 = 40$</p>	<p>Number lines, counting sticks and bar models should be used to show <u>representation</u> of counting in multiples.</p> 	<p>Count in multiples of a number aloud.</p> <p>Write sequences with multiples of numbers.</p> <p>0, 2, 4, 6, 8, 10 0, 3, 6, 9, 12, 15 0, 5, 10, 15, 20, 25, 30</p> <p>$4 \times 3 = \square$</p>
<p>Multiplication is commutative</p>	<p>Create arrays using counters and cubes and Numicon.</p>  <p>Pupils should understand that an array can represent different equations and that, as multiplication is commutative, the order of the multiplication does not affect the answer.</p> 	<p>Use representations of arrays to show different calculations and explore commutativity.</p> 	<p>$12 = 3 \times 4$ $12 = 4 \times 3$</p> <p>Use an array to write multiplication sentences and reinforce repeated addition.</p>  <p>$5 + 5 + 5 = 15$ $3 + 3 + 3 + 3 + 3 = 15$ $5 \times 3 = 15$ $3 \times 5 = 15$</p>

Using the Inverse

This should be taught alongside division, so pupils learn how they work alongside each other.

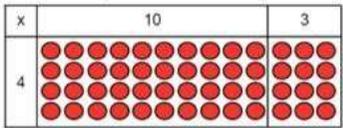
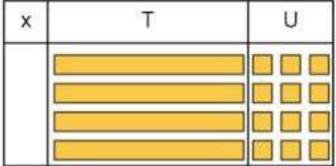
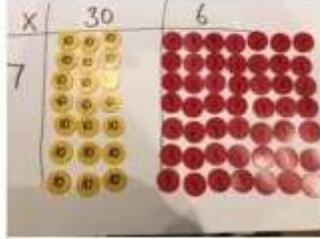
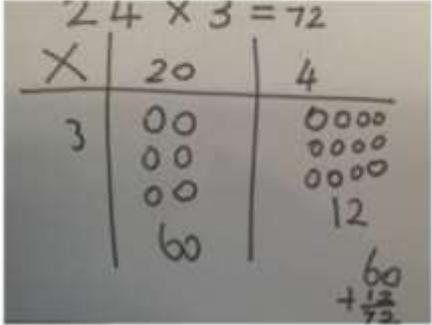
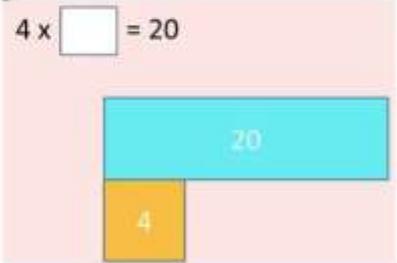
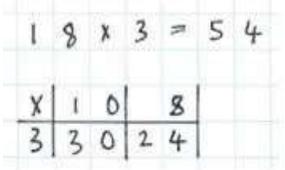


- $2 \times 4 = 8$
 - $4 \times 2 = 8$
 - $8 \div 2 = 4$
 - $8 \div 4 = 2$
 - $8 = 2 \times 4$
 - $8 = 4 \times 2$
 - $2 = 8 \div 4$
 - $4 = 8 \div 2$
- Show all 8 related fact family sentences.

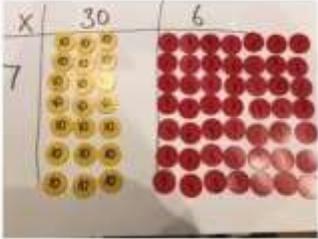
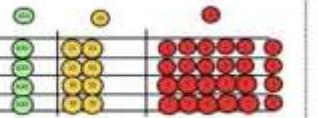
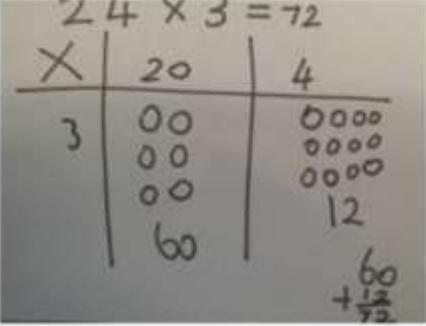
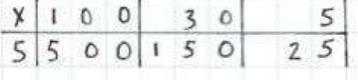
Vocabulary

Groups of, lots of, times, array, altogether, multiply, multiplied by, repeated addition, sets of, equal groups, times as big as, commutative.

Multiplication- Year 3

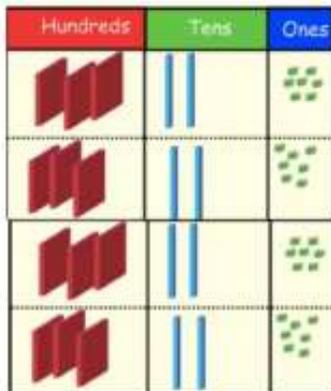
Objective and Strategy	Concrete	Pictorial	Abstract				
<p><i>Multiplying two-digit number by a one digit number</i></p> <p>Grid method progressing to the formal method.</p> <p>Solving problems including missing number problems, integer scaling problems.</p>	<p>Show the link with arrays to first introduce the grid method.</p>  <p>4 rows of 10 4 rows of 3</p> <p>Move on to using Base 10 to move towards a more compact method.</p>  <p>4 rows of 13</p> <p>Move on to place value counters to show how we are finding groups of a number.</p>  <p>Add up each column, starting with the ones making any exchanges needed.</p> <p>The calculation will be shown alongside the model chosen to see the connection</p> <table border="1" data-bbox="443 1193 719 1326"> <thead> <tr> <th>Model</th> <th>Calculation</th> </tr> </thead> <tbody> <tr> <td> </td> <td> </td> </tr> </tbody> </table>	Model	Calculation			<p>Children can represent their work with place value counters in a way that they understand.</p> <p>They can draw the counters using colours to show different amounts or just use the circles in the different columns to show their thinking as shown below.</p>  <p>Bar model are used to explore missing numbers</p> 	<p>Start with multiplying by one digit numbers and showing the clear addition alongside the grid.</p> <p>TO x O</p>  <p>Children to add up each column to find the answer.</p>
Model	Calculation						
<p>Vocabulary</p>	<p>Groups of, lots of, times, array, altogether, multiply, multiplied by, repeated addition, sets of, equal groups, times as big as, commutative, product, multiples of, scale up</p>						

Multiplication- Year 4

Objective and Strategy	Concrete	Pictorial	Abstract
<p>Multiply two-digit and three-digit numbers by a one-digit number using formal written layout</p> <p>Grid method recap from year 3 for 2 digits x 1 digit</p> <p>Multiplying numbers by 1 digit (year 4 expectation)</p>	 <p>Move on to place value counters to show how we are finding groups of a number. We are multiplying by 4 so we need 4 rows.</p>  <p>Calculators: 4×126</p> <p>Fill each row with 126.</p>  <p>Calculators: 4×126</p> <p>Add up each column, starting with the ones making any exchanges needed.</p>  <p>Then you have your answer.</p> 	<p>Children can represent their work with place value counters in a way that they understand.</p> <p>They can draw the counters using colours to show different amounts or just use the circles in the different columns to show their thinking as shown below.</p> 	<p>HTO x O</p>   <p>Children to add up each column to find the answer.</p>

Column multiplication

Children can continue to be supported by place value counters at the stage of multiplication. This initially done where there is no regrouping. $321 \times 2 = 642$



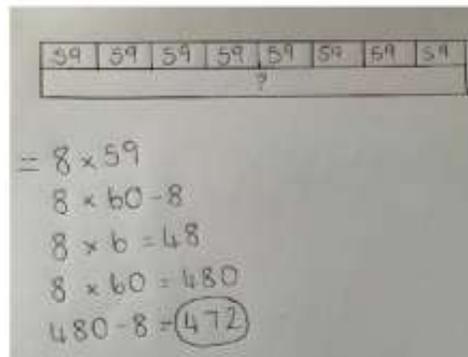
It is important at this stage that they always multiply the ones first.

The corresponding long multiplication is modelled alongside

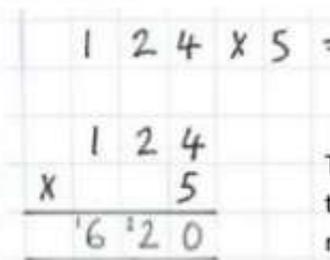
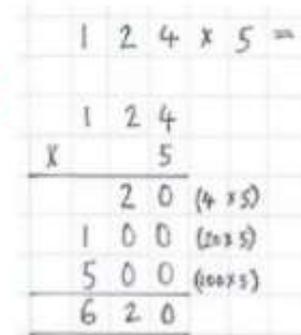
Model	Calculation

This grid method may be used to show how this relates to a formal written method.

x	100	20	4
5	500	100	20



Bar modelling and number lines can support learners when solving problems with multiplication alongside the formal written methods.



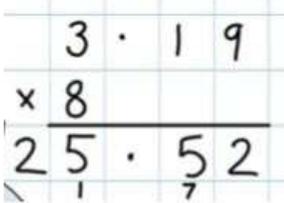
This may lead to a compact method.

Vocabulary Groups of, lots of, times, array, altogether, multiply, multiplied by, repeated addition, sets of, equal groups, times as big as, commutative, product, multiples of, scale up, inverse, derive

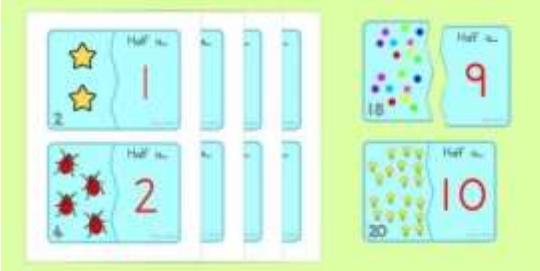
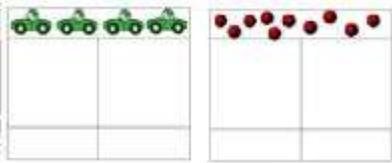
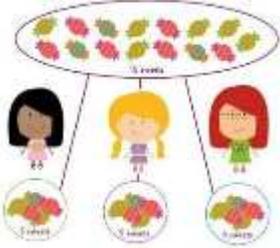
Multiplication Year 5

Objective and Strategy	Concrete	Pictorial	Abstract																																
<p>Multiply numbers up to 4-digits by a one-digit number using the format written method, including long multiplication for 2-digit numbers</p> <p>Column multiplication for 3 and 4 digits x 1 digit</p>	<p>Children can continue to be supported by place value counters at the stage of multiplication. This initially done where there is no regrouping. $321 \times 2 = 642$</p> <table border="1" data-bbox="331 284 593 590"> <tr> <td>Hundreds</td> <td>Tens</td> <td>Ones</td> </tr> <tr> <td></td> <td></td> <td></td> </tr> </table> <p>It is important at this stage that they always multiply the ones first.</p> <p>The corresponding long multiplication is modelled alongside</p>	Hundreds	Tens	Ones													<table border="1" data-bbox="922 183 1211 255"> <tr> <td>x</td> <td>300</td> <td>20</td> <td>7</td> </tr> <tr> <td>4</td> <td>1200</td> <td>80</td> <td>28</td> </tr> </table> 	x	300	20	7	4	1200	80	28	<table data-bbox="1422 183 1523 430"> <tr> <td>327</td> </tr> <tr> <td>x 4</td> </tr> <tr> <td>28</td> </tr> <tr> <td>80</td> </tr> <tr> <td>1200</td> </tr> <tr> <td>1308</td> </tr> </table>  <table data-bbox="1422 470 1624 630"> <tr> <td>327</td> </tr> <tr> <td>x 4</td> </tr> <tr> <td>1308</td> </tr> </table> <p>This may lead to a compact method.</p> <p>This may lead to a compact method.</p>	327	x 4	28	80	1200	1308	327	x 4	1308
Hundreds	Tens	Ones																																	
x	300	20	7																																
4	1200	80	28																																
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x 4																																			
1308																																			
<p>Column multiplication (long multiplication)</p>	<p>Manipulatives may still be used with the corresponding long multiplication modelled alongside</p> <table border="1" data-bbox="421 798 689 917"> <thead> <tr> <th>Model</th> <th>Calculation</th> </tr> </thead> <tbody> <tr> <td> </td> <td> </td> </tr> </tbody> </table>	Model	Calculation			<p>Moving forward, multiply by a 2 digit number showing the different rows within the grid method.</p> <p>$24 \times 16 = 384$</p> <table border="1" data-bbox="828 901 1153 1005"> <tr> <td>x</td> <td>20</td> <td>4</td> </tr> <tr> <td>10</td> <td>200</td> <td>40</td> </tr> <tr> <td>6</td> <td>120</td> <td>24</td> </tr> </table>	x	20	4	10	200	40	6	120	24	 <table data-bbox="1456 734 1601 965"> <tr> <td>24</td> </tr> <tr> <td>x 16</td> </tr> <tr> <td>144</td> </tr> <tr> <td>240</td> </tr> <tr> <td>384</td> </tr> </table> <p>24 x 6 on the first row. (6 x 4 = 24, carrying the 2 for the 20, then 6 x 2)</p> <p>24 x 10 on the second row. Show multiplying by 10 by putting zero in the units first.</p> <table data-bbox="1433 1077 1680 1252"> <tr> <td>1234</td> </tr> <tr> <td>x 16</td> </tr> <tr> <td>7404</td> </tr> <tr> <td>12340</td> </tr> <tr> <td>19744</td> </tr> </table> <p>(1234 x 6) (1234 x 10)</p>	24	x 16	144	240	384	1234	x 16	7404	12340	19744									
Model	Calculation																																		
x	20	4																																	
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<p>Vocabulary</p>	<p>Groups of, lots of, times, array, altogether, multiply, multiplied by, repeated addition, sets of, equal groups, times as big as, commutative, product, multiples of, scale up, inverse, derive, factor pairs, composite numbers, prime number, factors, squared, cubed</p>																																		

Multiplication- Year 6

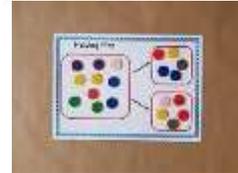
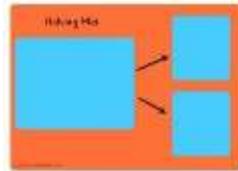
Objective and Strategy	Concrete	Pictorial	Abstract
Multiply decimal up to 2 decimal place by a single digit.			Remind children that the single digit belongs in the units column. Line up the decimal points in the question and the answer. 
vocabulary	Groups of, lots of, times, array, altogether, multiply, multiplied by, repeated addition, sets of, equal groups, times as big as, commutative, product, multiples of, scale up, inverse, derive, factor pairs, composite numbers, prime number, factors, squared, cubed		

Division- EYFS

Objectives	Concrete	Pictorial	Abstract
<p>Solve problems including halving and sharing.</p> <ul style="list-style-type: none"> Halving a whole, halving a quantity of objects. Sharing a quantity of objects. 	<div style="display: flex; justify-content: space-around;">   </div> <div style="text-align: center; margin-top: 10px;">  </div> <p style="margin-top: 10px;">Children have the opportunity to physically cut objects, food or shapes in half.</p>	<div style="background-color: #e0ffe0; padding: 10px; margin-bottom: 10px;">  </div> <p>Pictures and icons that encourage children to see concept of halving in relation to subitising, addition and subtraction knowledge. i.e. Knowing 4 is made of 2 groups of 2, so half of 4 is 2.</p> <div style="text-align: center; margin-bottom: 10px;">  </div> <p>Bar model with pictures or icons to support understanding of finding 2 equal parts of a number, to further understand how two halves make a whole.</p> <div style="display: flex; align-items: center; margin-bottom: 10px;">  <div style="margin-left: 20px;"> <p>Pictures for children to create and visualise 3 or more equal groups.</p> </div> </div>	



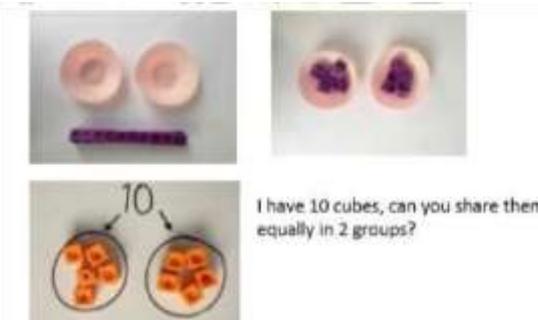
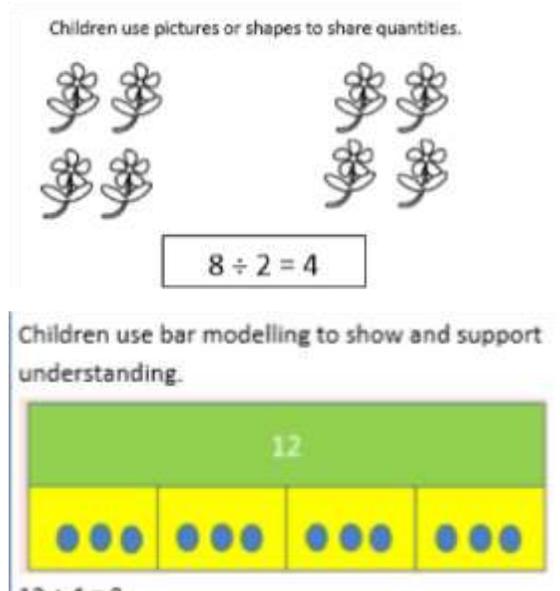
Use visual supports such as halving mats and part part whole, with the physical objects and resources that can be manipulated.



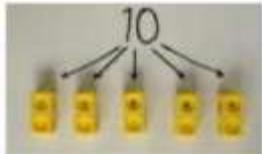
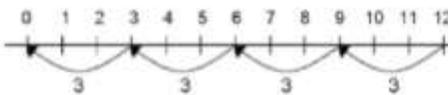
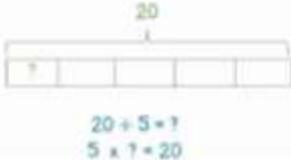
Counting and other maths resources for children to explore sharing between 3 or more.

Counting and other maths resources for children to share into two equal groups.

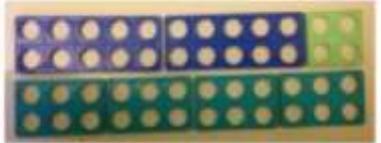
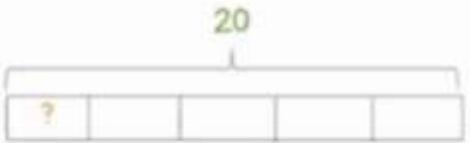
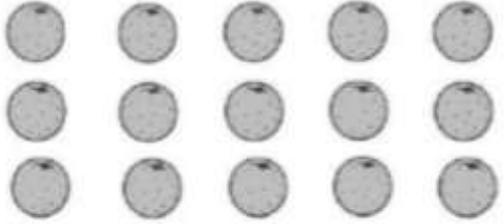
Division- Year 1

Objective and Strategy	Concrete	Pictorial	Abstract
<p>Division as sharing (sharing objects into groups)</p>	 <p style="font-size: small;">I have 10 cubes, can you share them equally in 2 groups?</p>	<p style="font-size: x-small;">Children use pictures or shapes to share quantities.</p>  <p style="font-size: x-small;">Children use bar modelling to show and support understanding.</p>	<p>Share 9 buns between three people.</p> <p style="text-align: center; font-size: 1.2em;">$9 \div 3 = 3$</p>
<p>Vocabulary</p>	<p>share, share equally, one each, two each..., group, groups of, lots of, array</p>		

Division- Year 2

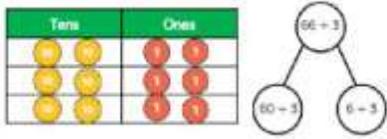
Objective and Strategy	Concrete	Pictorial	Abstract
Division as grouping	<p>Divide quantities into equal groups. Use cubes, counters, objects or place value counters to aid understanding.</p> <div style="display: flex; justify-content: space-around; align-items: center;"> <div style="text-align: center;">  </div> <div style="text-align: center;"> $96 \div 3 = 32$  </div> </div> <div style="display: flex; justify-content: space-around; align-items: center; margin-top: 10px;"> <div style="text-align: center;">  </div> </div>	<p>Use a number line to show jumps in groups. The number of jumps equals the number of groups.</p> <div style="text-align: center;">  </div> <p>Think of the bar as a whole. Split it into the number of groups you are dividing by and work out how many would be within each group.</p> <div style="text-align: center; margin-top: 10px;">  </div>	<div style="border: 1px solid gray; padding: 20px; width: 80%; margin: 0 auto;"> <p>$28 \div 7 = 4$</p> <p>Divide 28 into 7 groups. How many are in each group?</p> </div>
Vocabulary	share, share equally, one each, two each..., group, groups of, lots of, array, divide, divided by, divided into, division, grouping, number line, left, left over		

Division- Year 3

Objective and Strategy	Concrete	Pictorial	Abstract
<p>Division as grouping</p>	<p>Use cubes, counters, objects or place value counters to aid understanding.</p>  <p>24 divided into groups of 6 = 4</p> <p>$96 \div 3 = 32$</p> 	<p>Continue to use bar modelling to aid solving division problems.</p>  <p>$20 \div 5 = ?$ $5 \times ? = 20$</p>	<p>How many groups of 6 in 24?</p> <p>$24 \div 6 = 4$</p>
<p>Division with arrays</p>	 <p>Link division to multiplication by creating an array and thinking about the number sentences that can be created.</p> <p>Eg $15 \div 3 = 5$ $5 \times 3 = 15$ $15 \div 5 = 3$ $3 \times 5 = 15$</p>	<p>Draw an array and use lines to split the array into groups to make multiplication and division sentences</p> 	<p>Find the inverse of multiplication and division sentences by creating eight linking number sentences.</p> <p>$7 \times 4 = 28$ $4 \times 7 = 28$ $28 \div 7 = 4$ $28 \div 4 = 7$ $28 = 7 \times 4$ $28 = 4 \times 7$ $4 = 28 \div 7$ $7 = 28 \div 4$</p>

Divide 2digit numbers by a 1digit number by partitioning into tens and ones using a pv grid

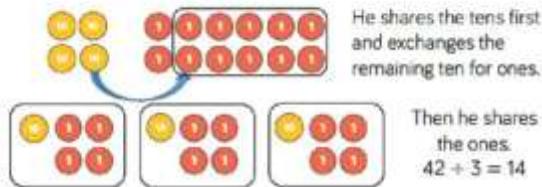
Eva uses a place value grid and part-whole model to solve $66 \div 3$



See part- whole model

Divide numbers that involve exchanging between the tens and ones. The answers donot have remainders.

Ron uses place value counters to divide 42 into three equal groups



Annie uses a similar method to divide 42 by 3



Children may use pictorial representation for the pv counters, alongside the part-whole model

Children use their times-tables to partition the number into multiples of the divisor.

$$96 \div 8$$

$$96 \div 4$$

$$96 \div 3$$

$$96 \div 6$$

Compare the statements using <, > or =

$$48 \div 4 \bigcirc 36 \div 3$$

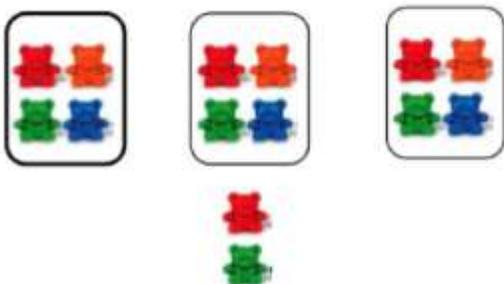
$$52 \div 4 \bigcirc 42 \div 3$$

$$60 \div 3 \bigcirc 60 \div 4$$

Division with a remainder

$$14 \div 3 =$$

Divide objects between groups and see how much is left over



Use place value counters to work out $94 \div 4$. Did you need to exchange any tens for ones? Is there a remainder?



Tens	Ones

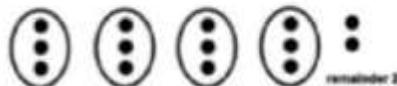
29

Moving on to:

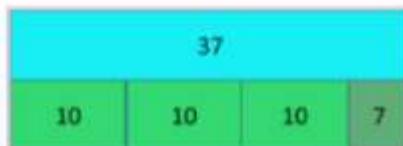
Jump forward in equal jumps on a number line then see how many more you need to jump to find a remainder.



Draw dots and group them to divide an amount and clearly show a remainder.



Use bar models to show division with remainders.



Complete written divisions and show the remainder using r.

$$29 \div 8 = 3 \text{ REMAINDER } 5$$

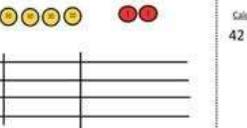
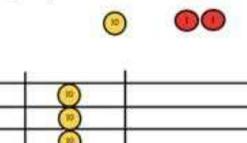
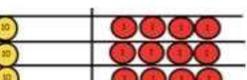
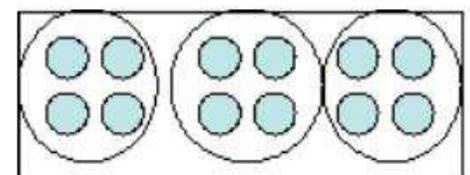
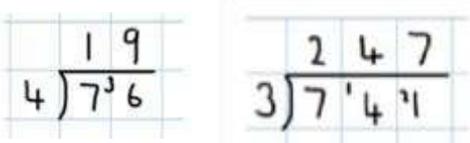
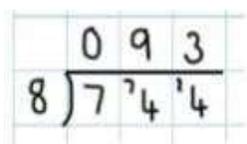
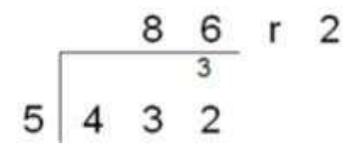
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dividend
divisor
quotient
remainder

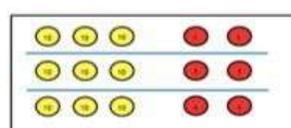
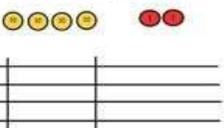
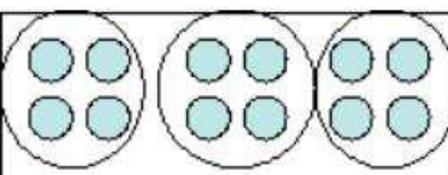
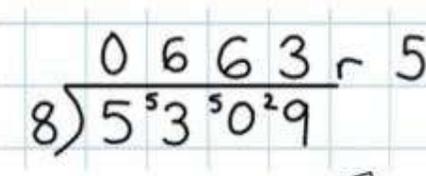
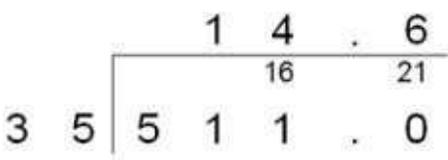
Vocabulary

share, share equally, one each, two each..., group, groups of, lots of, array, divide, divided by, divided into, division, grouping, number line, left, left over, product

Division- Year 4

Objective and Strategy	Concrete	Pictorial	Abstract				
<p>Divide up to 3 digit numbers by 1 digit. Short Division</p>	<p>$96 \div 3$</p> <table style="margin-left: auto; margin-right: auto; border-collapse: collapse;"> <tr> <td style="text-align: center; padding: 0 10px;">Tens</td> <td style="text-align: center; padding: 0 10px;">Units</td> </tr> <tr> <td style="text-align: center;">3</td> <td style="text-align: center;">2</td> </tr> </table>  <p>Use place value counters to divide using the bus stop method alongside</p>  <p>$42 \div 3 =$</p> <p>Start with the biggest place value, we are sharing 40 into three groups. We can put 1 ten in each group and we have 1 ten left over.</p>  <p>We exchange this ten for ten ones and then share the ones equally among the groups.</p>  <p>We look how much in 1 group so the answer is 14.</p>	Tens	Units	3	2	<p>Students can continue to use drawn diagrams with dots or circles to help them divide numbers into equal groups.</p>  <p>Encourage them to move towards counting in multiples to divide more efficiently.</p>	<p>Begin with divisions that divide equally with no remainder</p>  <p>Children should be aware that a 0 is used to keep place value, if the number is not divisible.</p>  <p>Move onto divisions with a remainder.</p> 
Tens	Units						
3	2						
<p>Vocabulary</p>	<p>share, share equally, one each, two each..., group, groups of, lots of, array, divide, divided by, divided into, division, grouping, number line, left, left over, product, division facts, inverse, derive</p>						

Division- Year 5

Objective and Strategy	Concrete	Pictorial	Abstract				
<p><i>Divide at least 4 digit numbers by 1 digit.</i></p> <p><i>Interpret remainders appropriately for the context</i></p> <p>Short Division</p>	<p>$96 \div 3$</p> <table style="margin-left: auto; margin-right: auto; border-collapse: collapse;"> <tr> <td style="padding: 0 10px;">Tens</td> <td style="padding: 0 10px;">Units</td> </tr> <tr> <td style="text-align: center;">3</td> <td style="text-align: center;">2</td> </tr> </table>  <p>Use place value counters to divide using the bus stop method alongside</p>  <p style="font-size: small;">Calculations: $42 \div 3 =$</p> <p>$42 \div 3 =$</p> <p>Start with the biggest place value, we are sharing 40 into three groups. We can put 1 ten in each group and we have 1 ten left over.</p>  <p>We exchange this ten for ten ones and then share the ones equally among the groups.</p>  <p>We look how much in 1 group so the answer is 14.</p>	Tens	Units	3	2	<p>Students can continue to use drawn diagrams with dots or circles to help them divide numbers into equal groups.</p>  <p>Encourage them to move towards counting in multiples to divide more efficiently.</p>	 <p>Finally move into decimal places to divide the total accurately.</p> 
Tens	Units						
3	2						
Vocabulary	<p>share, share equally, one each..., group, groups of, lots of, array, divide, divided by, divided into, division, grouping, number line, left, left over, product, division facts, inverse, derive, formal written method.</p>						

Division-Year 6

Objective and Strategy

Abstract

Long Division

Step 1 – a remainder in the ones

$$\begin{array}{r} \text{h t o} \\ 041\text{R}1 \\ \hline 4 \overline{) 165} \end{array}$$

4 does not go into 1 (hundred). So combine the 1 hundred with the 6 tens (160).

4 goes into 16 four times.

4 goes into 5 once, leaving a remainder of 1.

$$\begin{array}{r} \text{th h t o} \\ 0400\text{R}7 \\ \hline 8 \overline{) 3207} \end{array}$$

8 does not go into 3 of the thousands. So combine the 3 thousands with the 2 hundreds (3,200)

8 goes into 32 four times ($3,200 \div 8 = 400$)

8 goes into 0 zero times (tens)

8 goes into 7 zero times, and leaves a remainder of 7.

$$\begin{array}{r} \text{h t o} \\ 061 \\ \hline 4 \overline{) 247} \\ \underline{-4} \\ 3 \end{array}$$

When dividing the ones, 4 goes into 7 one time. Multiply $1 \times 4 = 4$, write that four under the 7, and subtract. This finds us the remainder of 3.

Check: $4 \times 61 + 3 = 247$

$$\begin{array}{r} \text{th h t o} \\ 0402 \\ \hline 4 \overline{) 1609} \\ \underline{-8} \\ 1 \end{array}$$

When dividing the ones, 4 goes into 9 two times. Multiply $2 \times 4 = 8$, write that eight under the 9, and subtract. This finds us the remainder of 1.

Check: $4 \times 402 + 1 = 1,609$

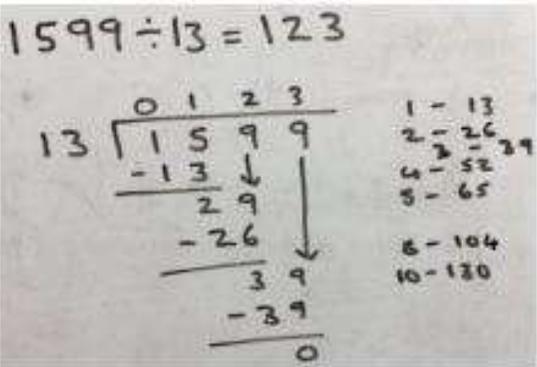
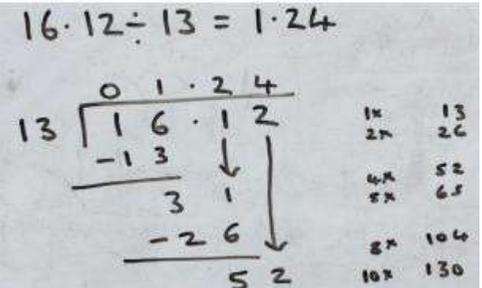
Step 2 – a remainder in the tens

1. Divide.	2. Multiply & subtract.	3. Drop down the next digit.
$\begin{array}{r} \text{t o} \\ 2 \overline{)58} \\ \underline{4} \\ 18 \end{array}$ <p>Two goes into 5 two times, or 5 tens ÷ 2 = 2 whole tens -- but there is a remainder!</p>	$\begin{array}{r} \text{t o} \\ 2 \overline{)58} \\ \underline{-4} \\ 1 \end{array}$ <p>To find it, multiply $2 \times 2 = 4$, write that 4 under the five, and subtract to find the remainder of 1 ten.</p>	$\begin{array}{r} \text{t o} \\ 2 \overline{)58} \\ \underline{-4} \\ 18 \end{array}$ <p>Next, drop down the 8 of the ones next to the leftover 1 ten. You combine the remainder ten with 8 ones, and get 18.</p>

1. Divide.	2. Multiply & subtract.	3. Drop down the next digit.
$\begin{array}{r} \text{t o} \\ 2 \overline{)58} \\ \underline{-4} \\ 18 \end{array}$ <p>Divide 2 into 18. Place 9 into the quotient.</p>	$\begin{array}{r} \text{t o} \\ 2 \overline{)58} \\ \underline{-4} \\ 18 \\ \underline{-18} \\ 0 \end{array}$ <p>Multiply $9 \times 2 = 18$, write that 18 under the 18, and subtract.</p>	$\begin{array}{r} \text{t o} \\ 2 \overline{)58} \\ \underline{-4} \\ 18 \\ \underline{-18} \\ 0 \end{array}$ <p>The division is over since there are no more digits in the dividend. The quotient is 29.</p>

Step 3 – a remainder in any of the place values

<p>1. Divide.</p>	<p>2. Multiply & subtract.</p>	<p>3. Drop down the next digit.</p>
$\begin{array}{r} \text{h t o} \\ 1 \\ 2 \overline{)278} \end{array}$ <p>Two goes into 2 one time, or 2 hundreds + 2 = 1 hundred.</p>	$\begin{array}{r} \text{h t o} \\ 1 \\ 2 \overline{)278} \\ -2 \\ \hline 0 \end{array}$ <p>Multiply $1 \times 2 = 2$, write that 2 under the two, and subtract to find the remainder of zero.</p>	$\begin{array}{r} \text{h t o} \\ 18 \\ 2 \overline{)278} \\ -2 \\ \hline 07 \end{array}$ <p>Next, drop down the 7 of the tens next to the zero.</p>
<p>Divide.</p>	<p>Multiply & subtract.</p>	<p>Drop down the next digit.</p>
$\begin{array}{r} \text{h t o} \\ 13 \\ 2 \overline{)278} \\ -2 \\ \hline 07 \end{array}$ <p>Divide 2 into 7. Place 3 into the quotient.</p>	$\begin{array}{r} \text{h t o} \\ 13 \\ 2 \overline{)278} \\ -2 \\ \hline 07 \\ -6 \\ \hline 1 \end{array}$ <p>Multiply $3 \times 2 = 6$, write that 6 under the 7, and subtract to find the remainder of 1 ten.</p>	$\begin{array}{r} \text{h t o} \\ 13 \\ 2 \overline{)278} \\ -2 \\ \hline 07 \\ -6 \\ \hline 18 \end{array}$ <p>Next, drop down the 8 of the ones next to the 1 leftover ten.</p>
<p>1. Divide.</p>	<p>2. Multiply & subtract.</p>	<p>3. Drop down the next digit.</p>
$\begin{array}{r} \text{h t o} \\ 139 \\ 2 \overline{)278} \\ -2 \\ \hline 07 \\ -6 \\ \hline 18 \end{array}$ <p>Divide 2 into 18. Place 9 into the quotient.</p>	$\begin{array}{r} \text{h t o} \\ 139 \\ 2 \overline{)278} \\ -2 \\ \hline 07 \\ -6 \\ \hline 18 \\ -18 \\ \hline 0 \end{array}$ <p>Multiply $9 \times 2 = 18$, write that 18 under the 18, and subtract to find the remainder of zero.</p>	$\begin{array}{r} \text{h t o} \\ 139 \\ 2 \overline{)278} \\ -2 \\ \hline 07 \\ -6 \\ \hline 18 \\ -18 \\ \hline 0 \end{array}$ <p>There are no more digits to drop down. The quotient is 139.</p>

<p>Divide numbers up to 4 digits by a two-digit whole number using the formal written method of division</p>	<div style="display: flex; justify-content: space-around;"> <div style="text-align: center;"> $1599 \div 13 = 123$  </div> <div style="text-align: center;"> $16.12 \div 13 = 1.24$  </div> </div>
<p>Vocabulary</p>	<p>share, share equally, one each, two each..., group, groups of, lots of, array, divide, divided by, divided into, division, grouping, number line, left, left over, product, division facts, inverse, derive, formal written method.</p>

Minimal Resources required to support the CPA approach (depending on year group):

- 10 frames (including egg boxes)
- Straws/pipe cleaners
- Bead strings (to 20 and 100)
- Base 10/Dienes
- Place value grids
- Double-sided counters
- Part-part whole templates
- Place value counters (KS2)
- Multi-link cubes